



# Global Modeling of the Space Environment System

**Alex Glocer**

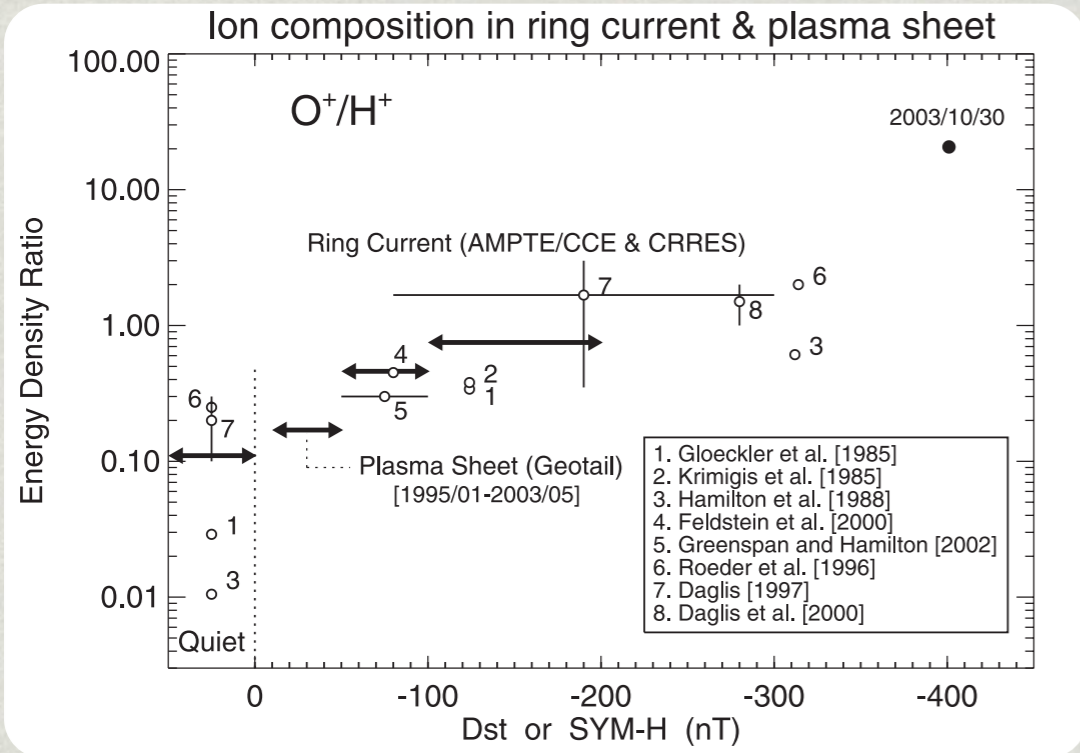
thanks to: J. Dorelli, L. Daldorff, G. Toth, D. Welling, G. Khazanov, C.Komar, L. Wang,

# Overview

- The space environment system is comprised of a myriad of constituents and regions with different:
  - Characteristic energies
  - Spatial and temporal scales
  - Physical processes
- Sometimes what is required is extending the equation set, and sometimes coupling tailored models is needed.
- Three topics covered:
  - Magnetosphere composition and ionospheric outflow
  - Inner magnetosphere coupling
  - Reconnection in global magnetosphere models
- I will cover these topics from a global modeling perspective.

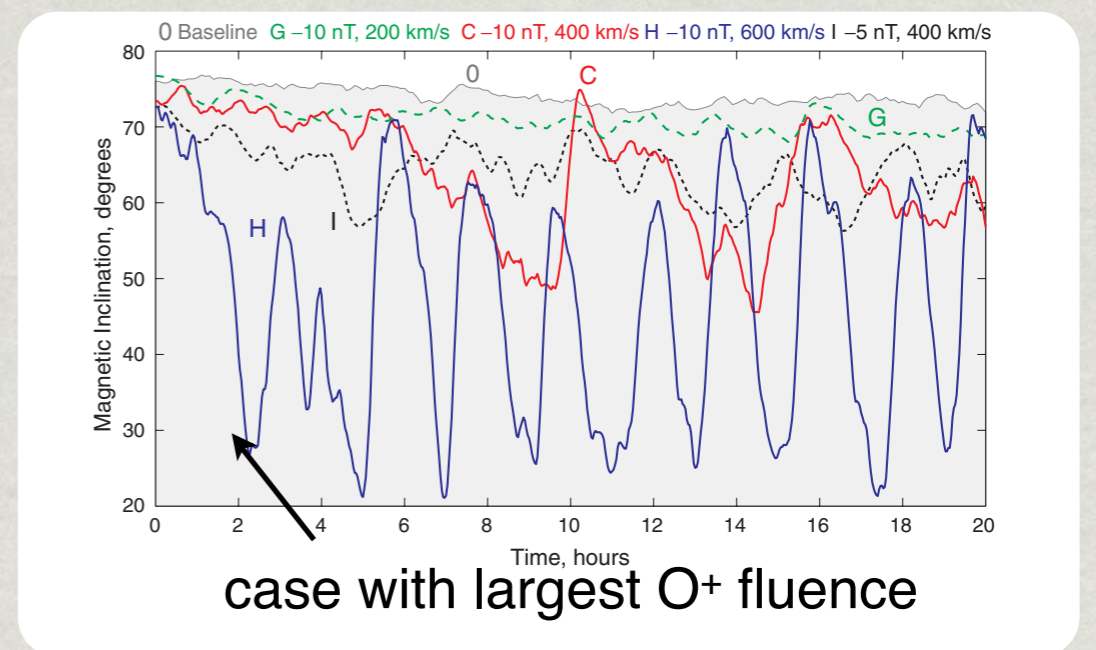
# O<sup>+</sup> in the ring Current

Nose et al. [2005]



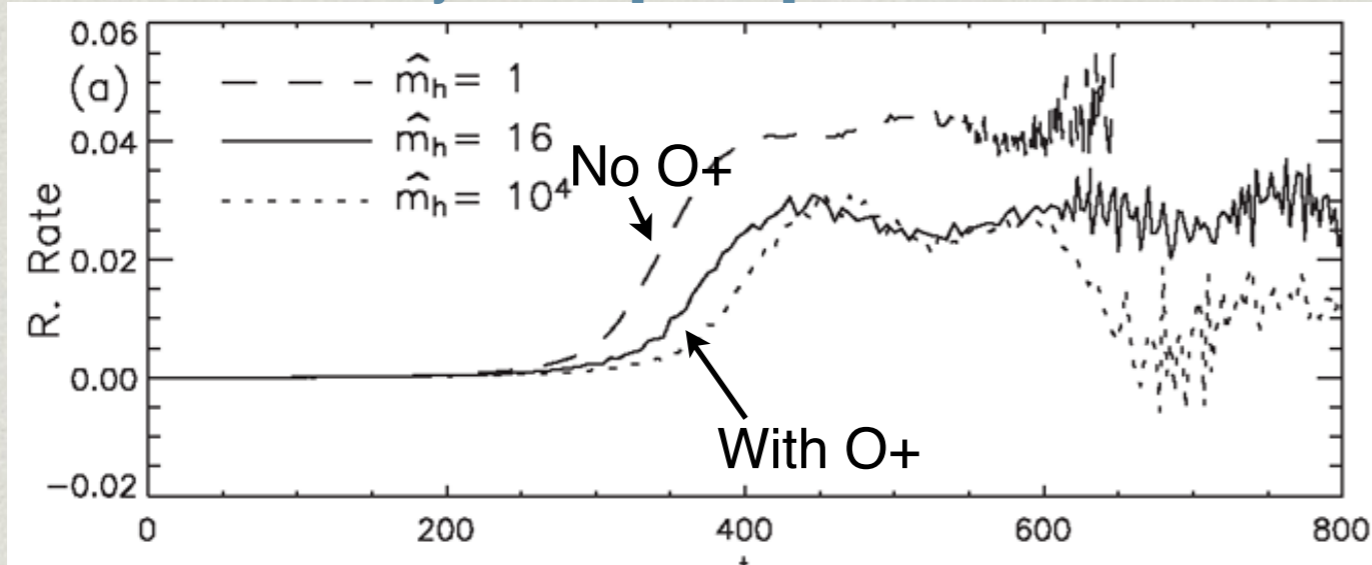
# O<sup>+</sup> with Sawteeth

Brambles et al. [2010]



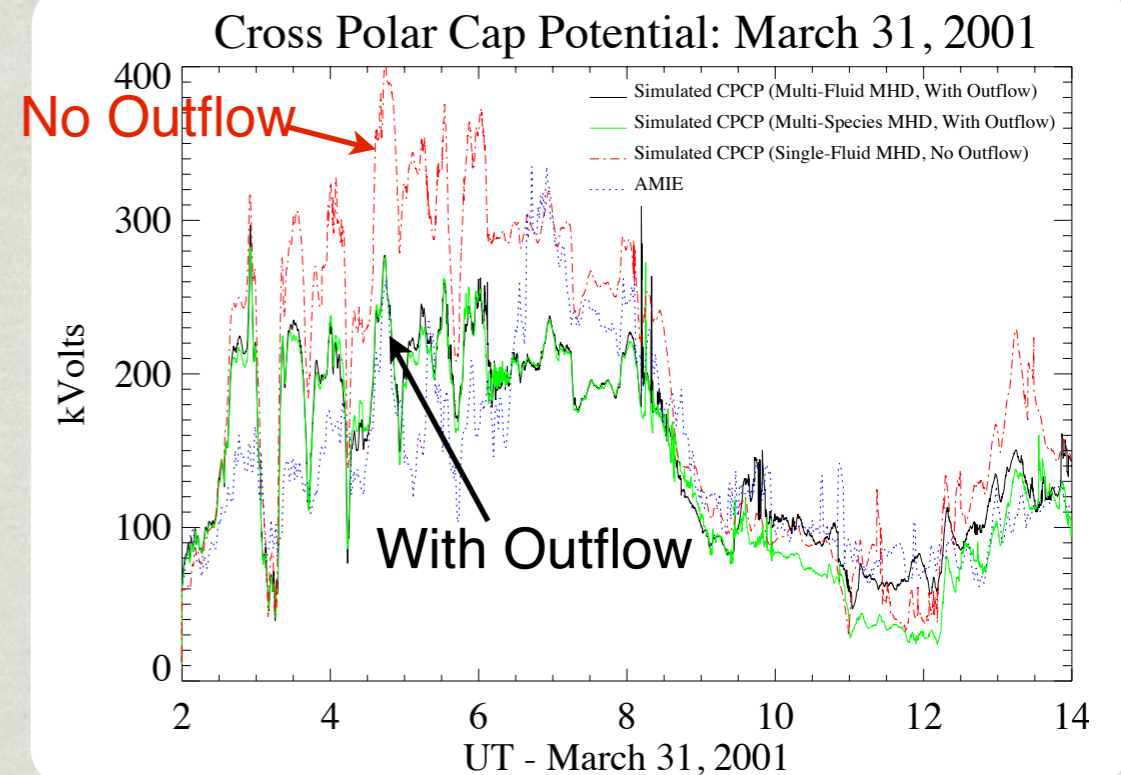
# O<sup>+</sup> and Reconnection

Shay et al. [2004]

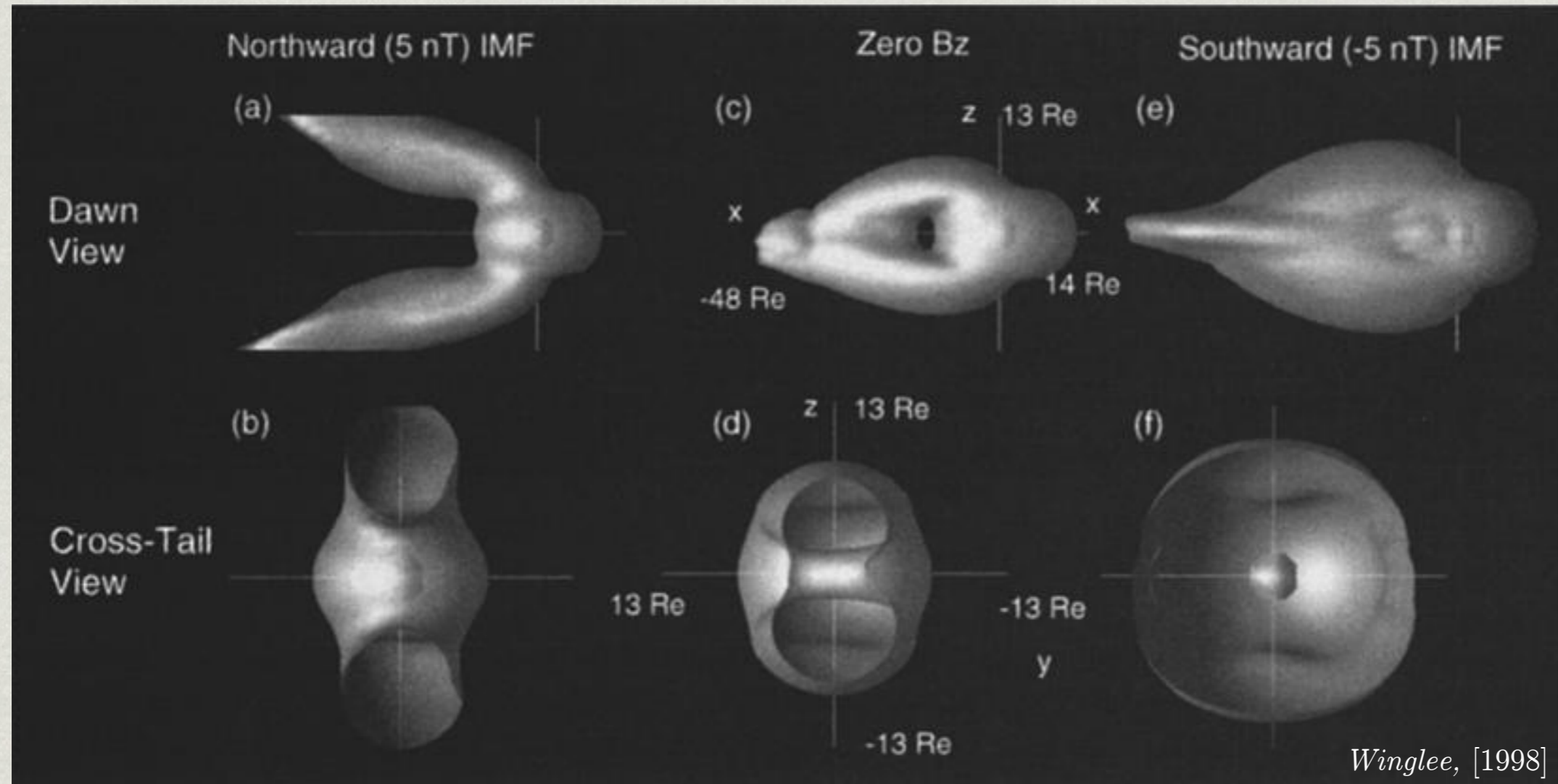


# O<sup>+</sup> and CPCP

Glocer et al. [2009]



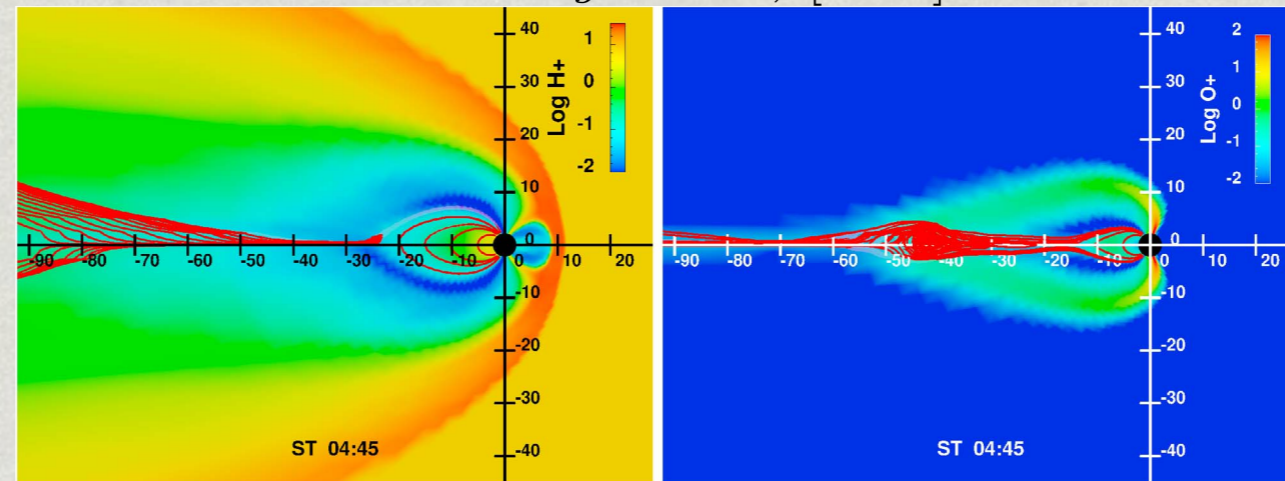
# First Multifluid MHD Modeling of the Magnetosphere



- Winglee [1998], first MFMHD simulations of the magnetosphere.
- Investigated geopause boundaries where the contributions to the magnetospheric density or pressure from the ionosphere equals that from the solar wind.

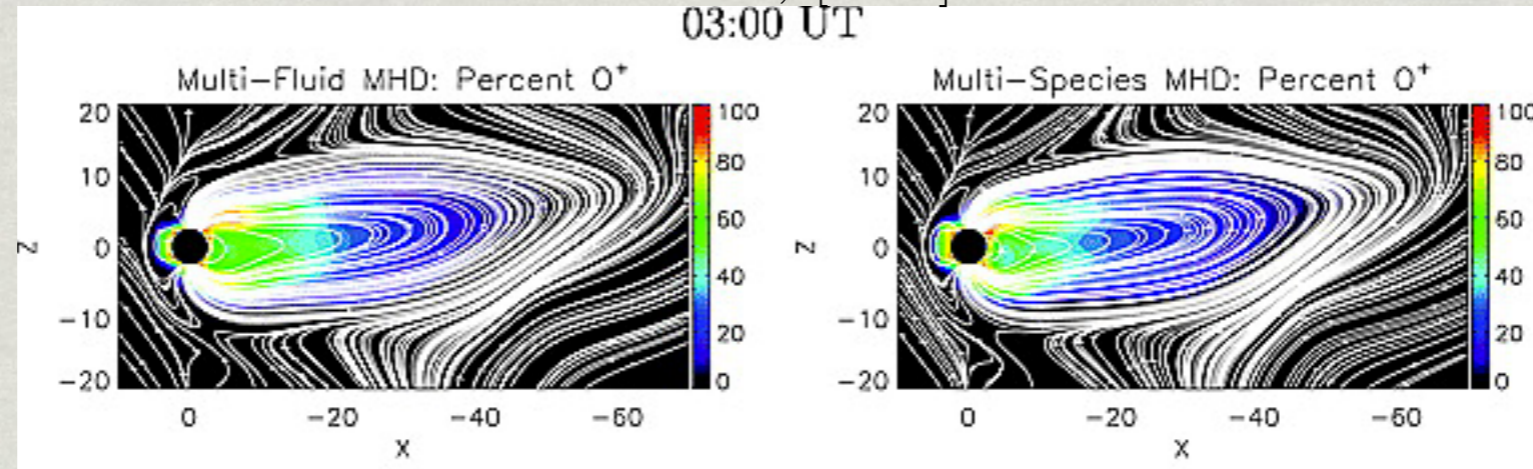
# 10 years later...

*Wiltberger et al, [2010]*



*Glocer et al, [2009]*

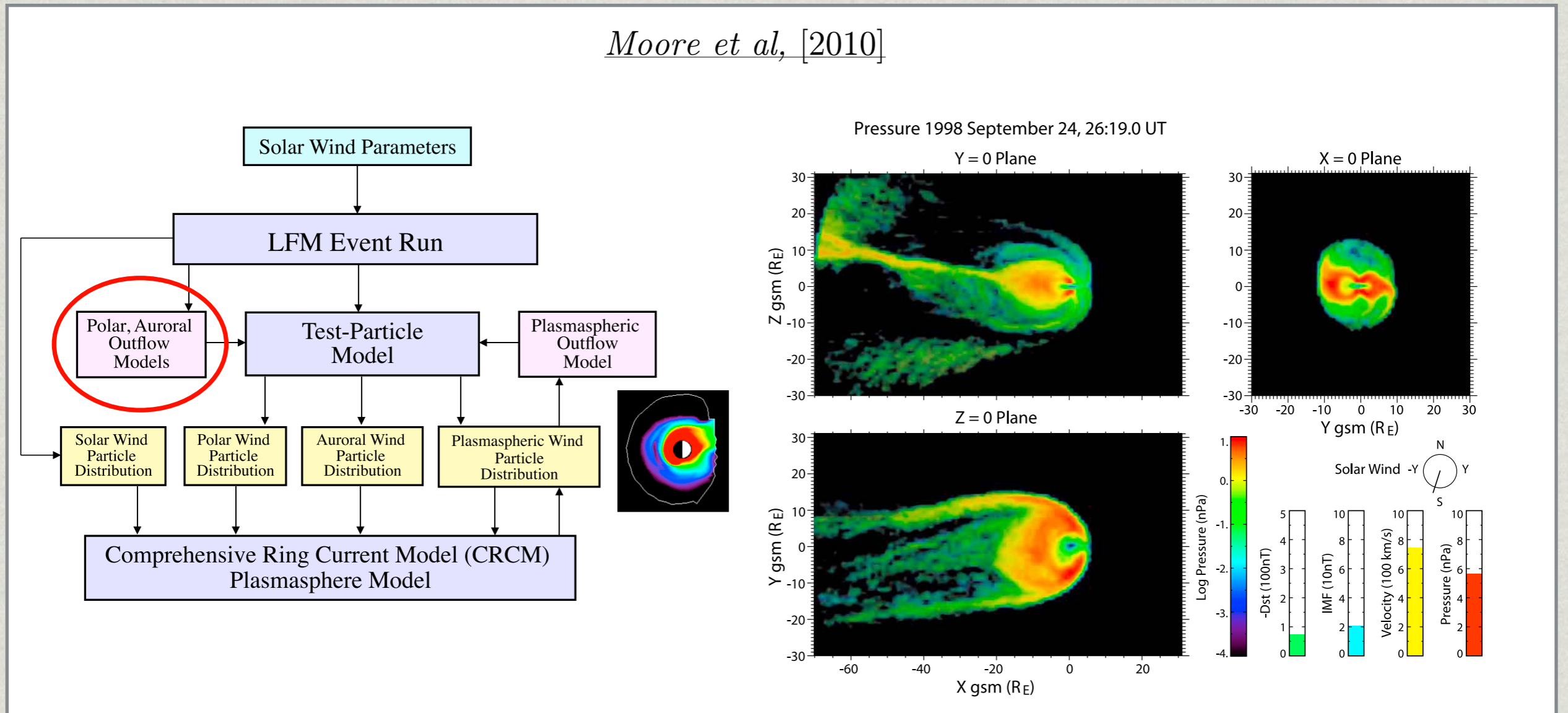
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- Both LFM and BATS-R-US global magnetosphere models now have multi fluid capabilities
- Used to investigate consequences of ionospheric outflow.

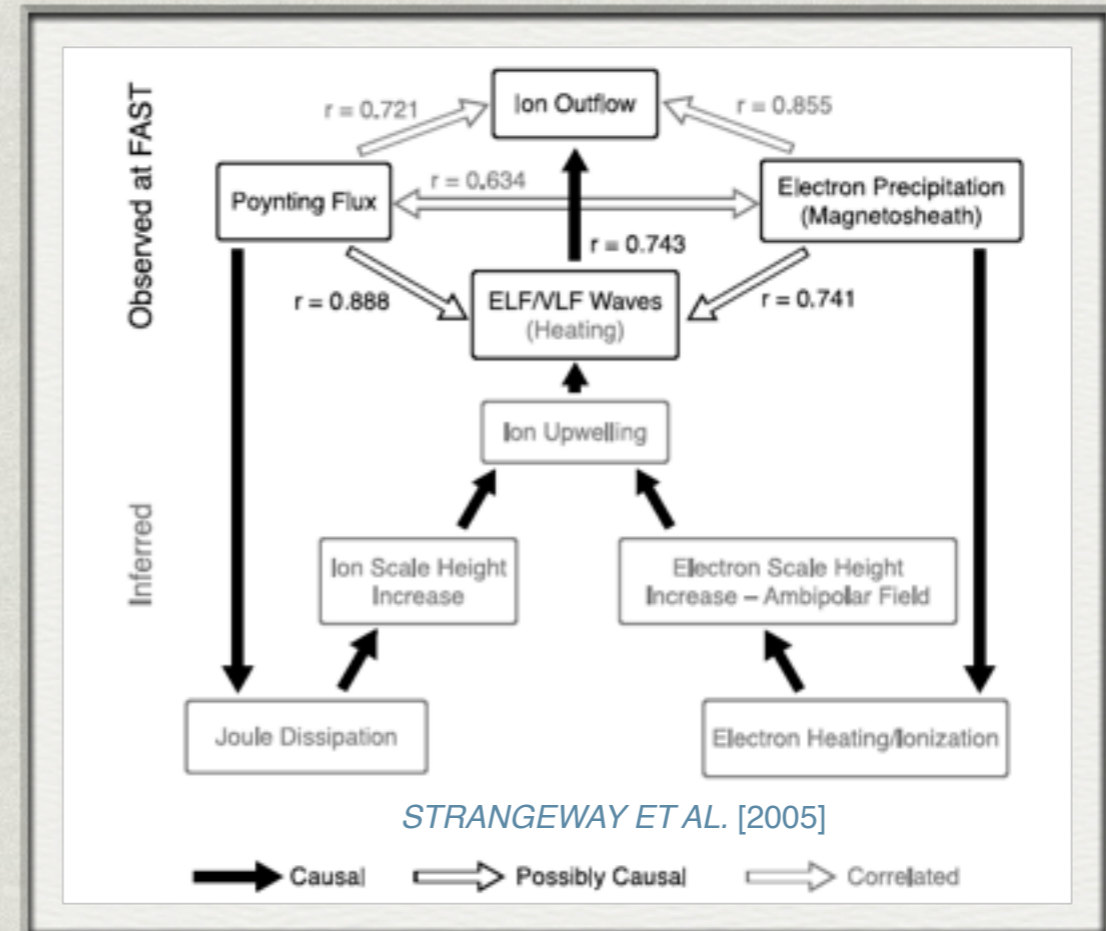
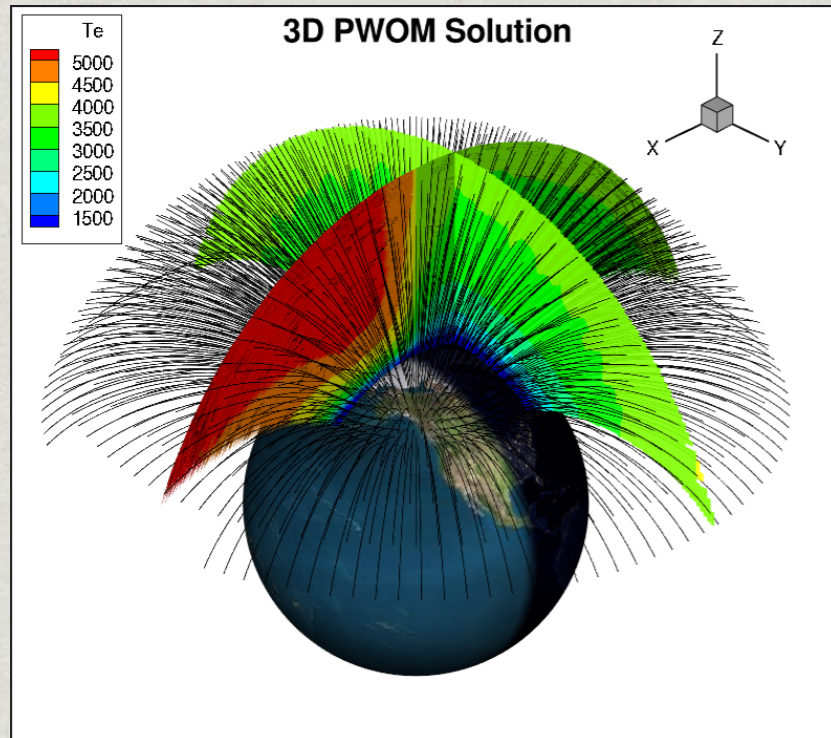
# Alternatives to Multifluid MHD

*Moore et al, [2010]*



- Using MHD simulation to provide the fields and using test particles to track outflow.
- Advantages: Test particles include non-fluid effects.
- Disadvantage: Fields do not evolve consistently with particle distributions.

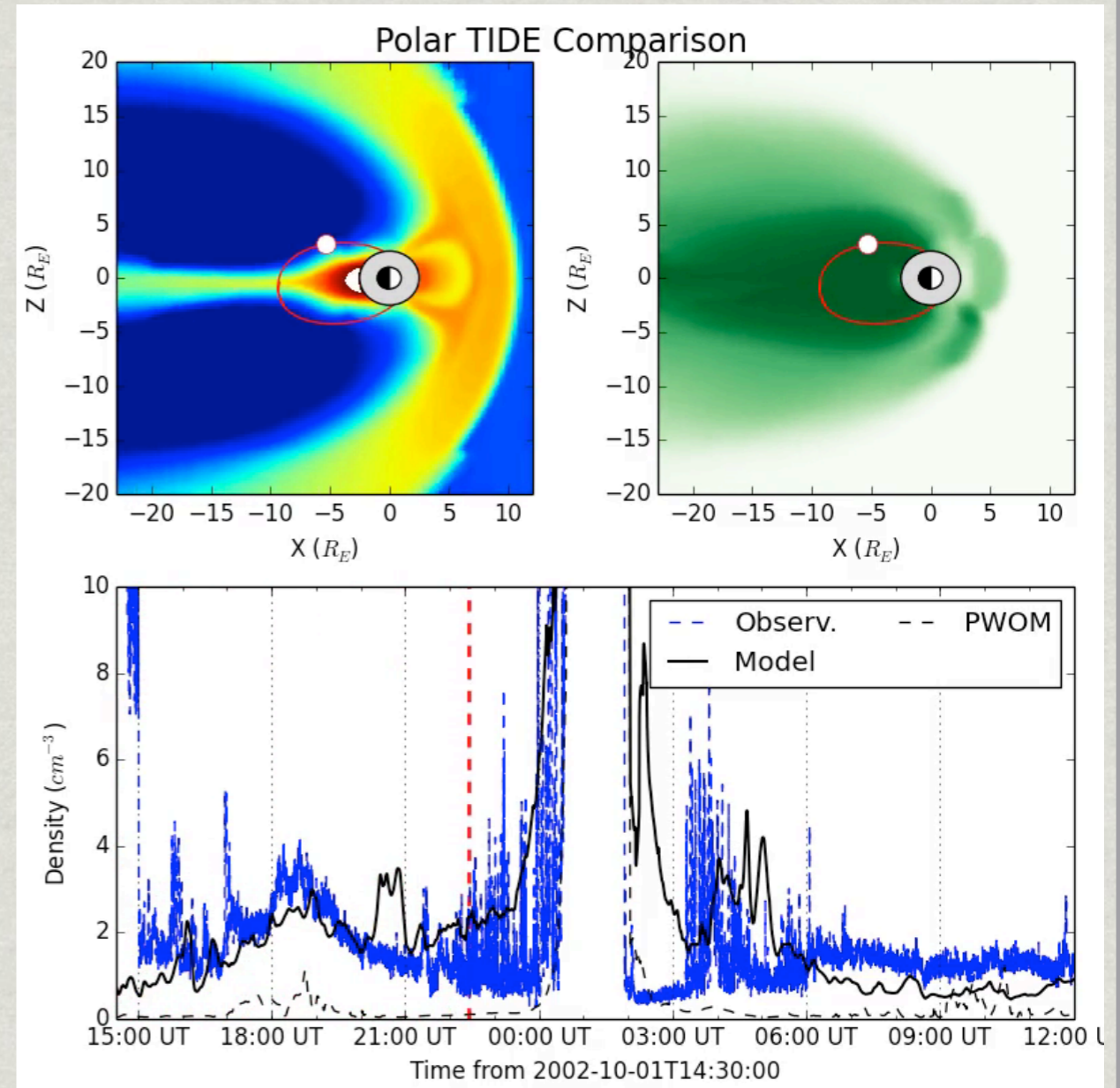
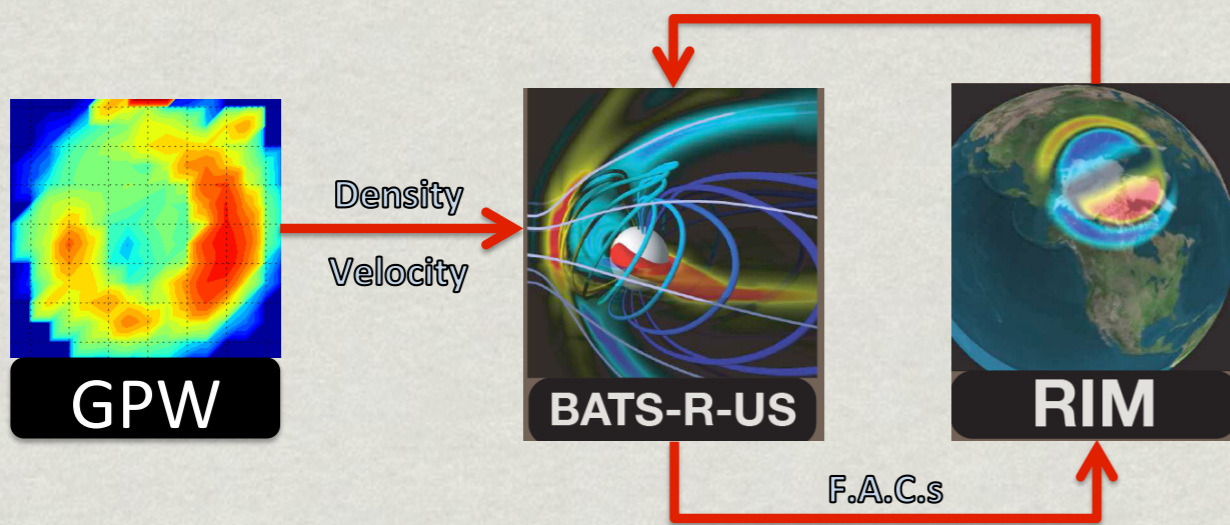
# Representing the Ionospheric Source



- There are pretty much three ways:
- 1) Just specify an inner boundary density and let the pressure gradients and diffusion handle it. (Winglee et al. [2004], Welling et al. [2013])
  - 2) Use of an empirical model
    - Easy to implement and reasonable representation of source
    - Great for use a source for understanding consequences of outflow
    - No physics so not good for studying causes of outflow
  - 3) First principles modeling (Glocer et al [2009 & 2012])
    - Great for trying to understand physics of outflow
    - Computationally expensive lots of physics to account for

# More and More Outflow Models are being Merged

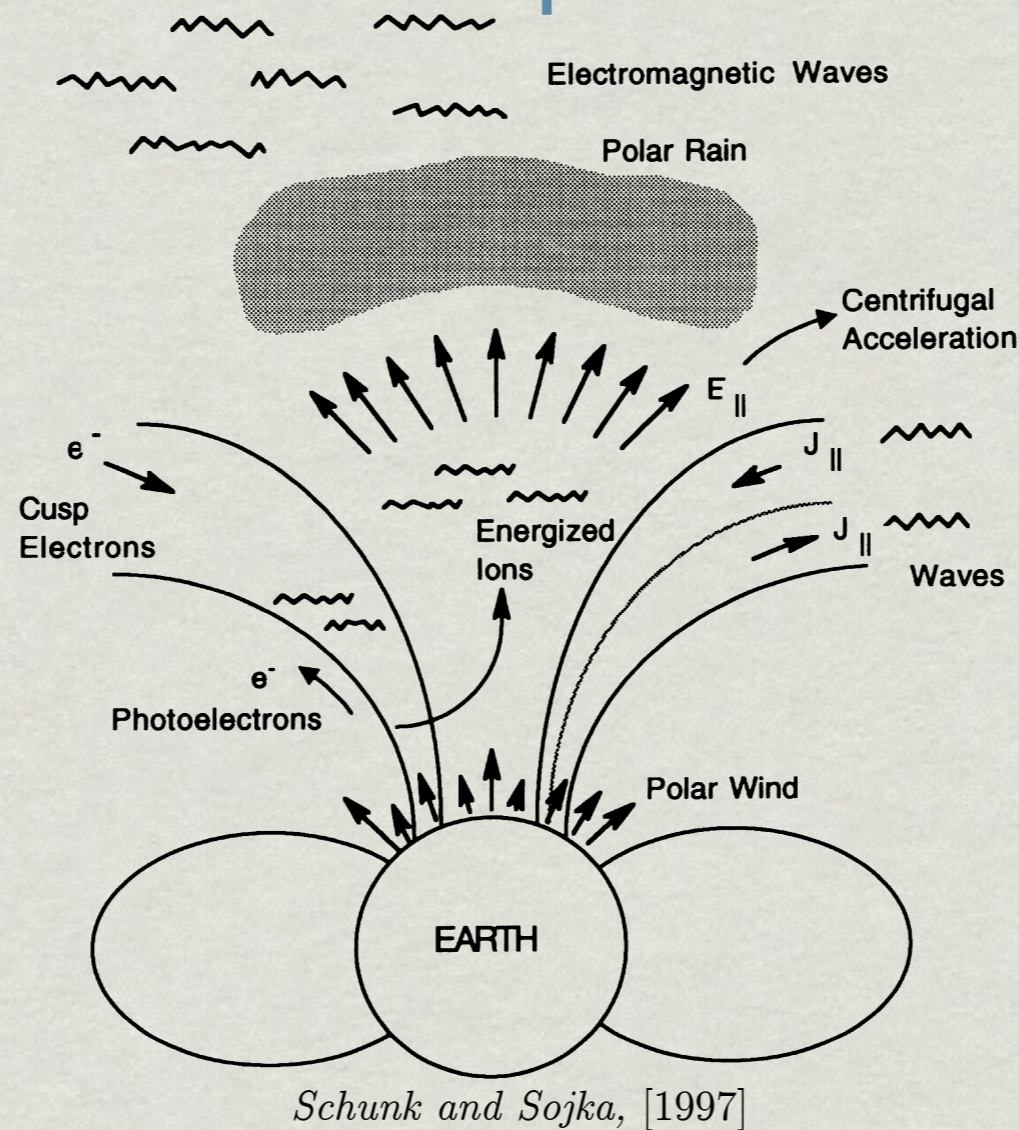
SWMF



Courtesy of D. Welling



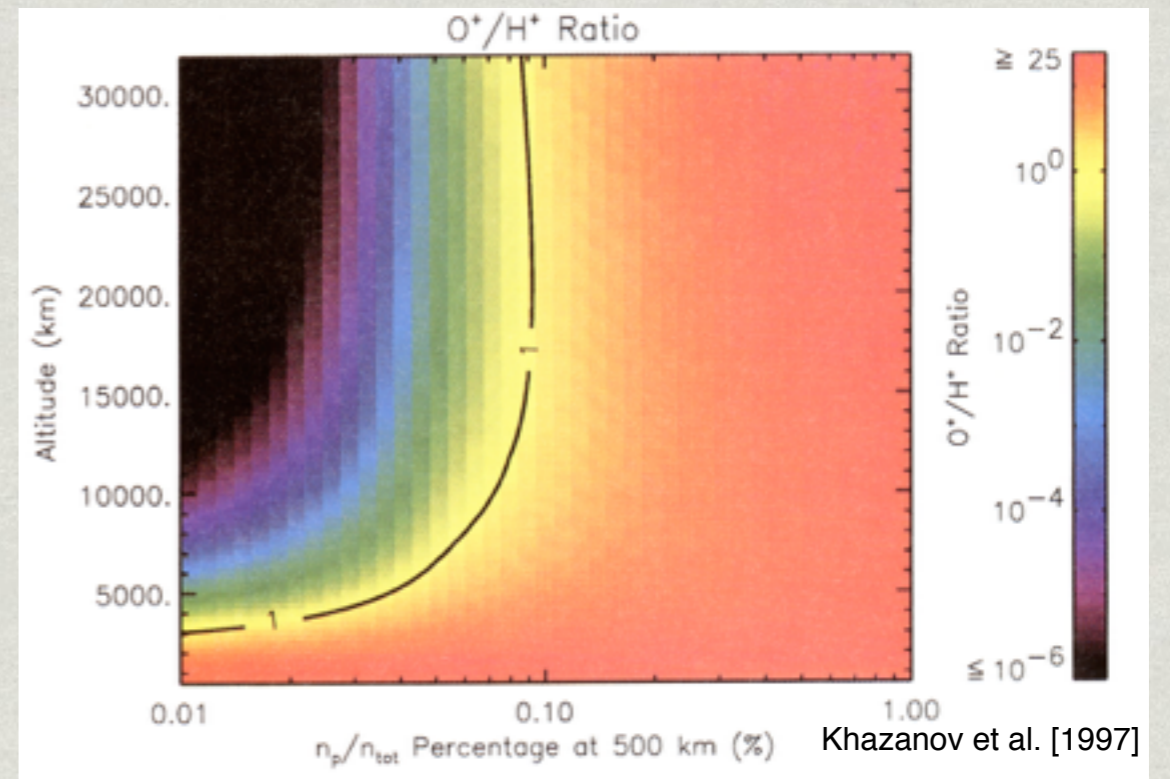
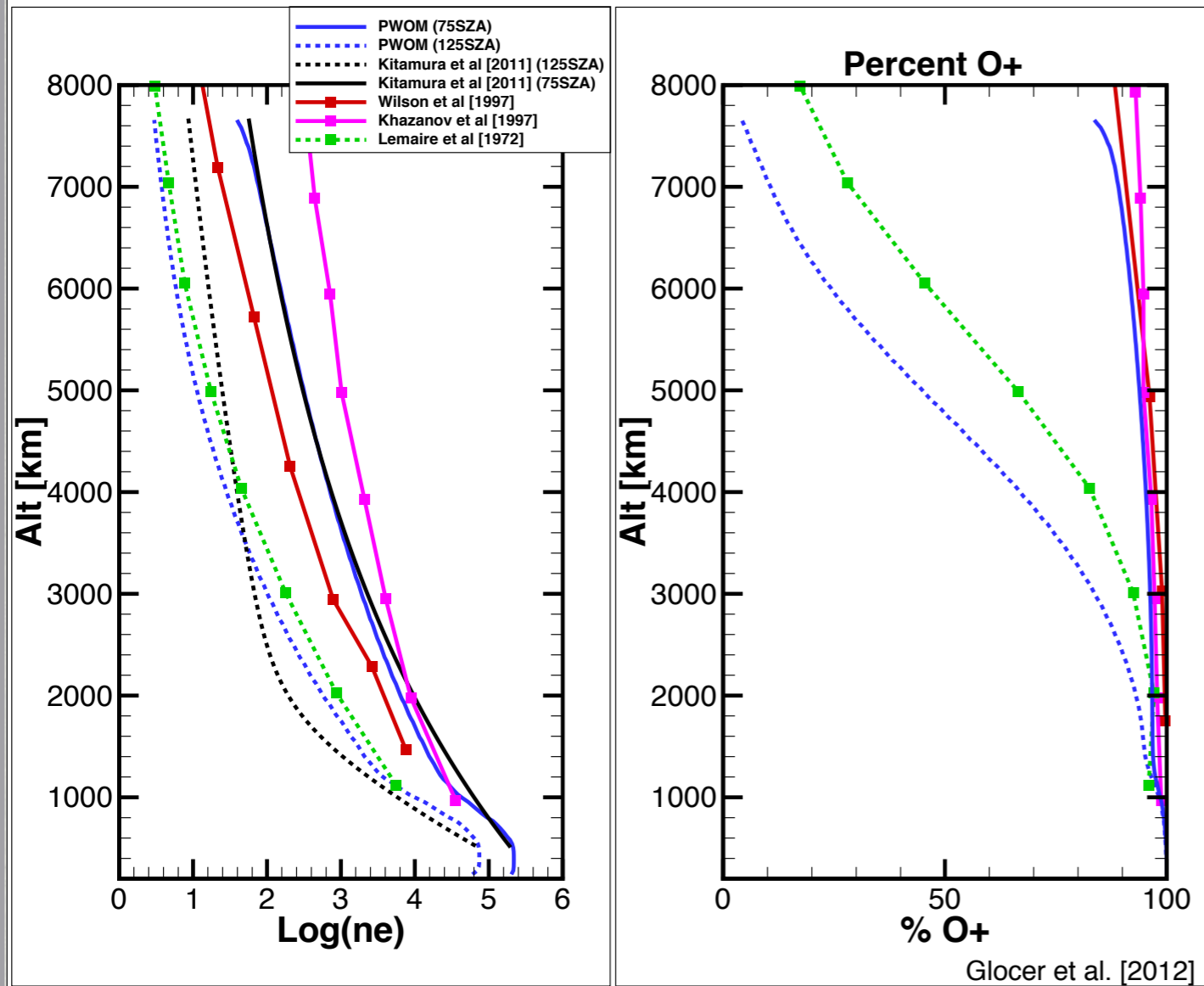
# Pathways of Ionospheric Outflow



- Superthermal Electrons (SEs) can reduce the potential barrier.
- Centrifugal force due to field line convection and curvature change.
- Transverse heating of ions as a result of WPI.
- Ponderomotive forces of Alfvén waves.
- Other less discussed mechanisms include FACs driving  $E_{||}$  and low altitude frictional heating driving upwelling.

# Effect of SEs on Outflow

Comparison with Past Studies

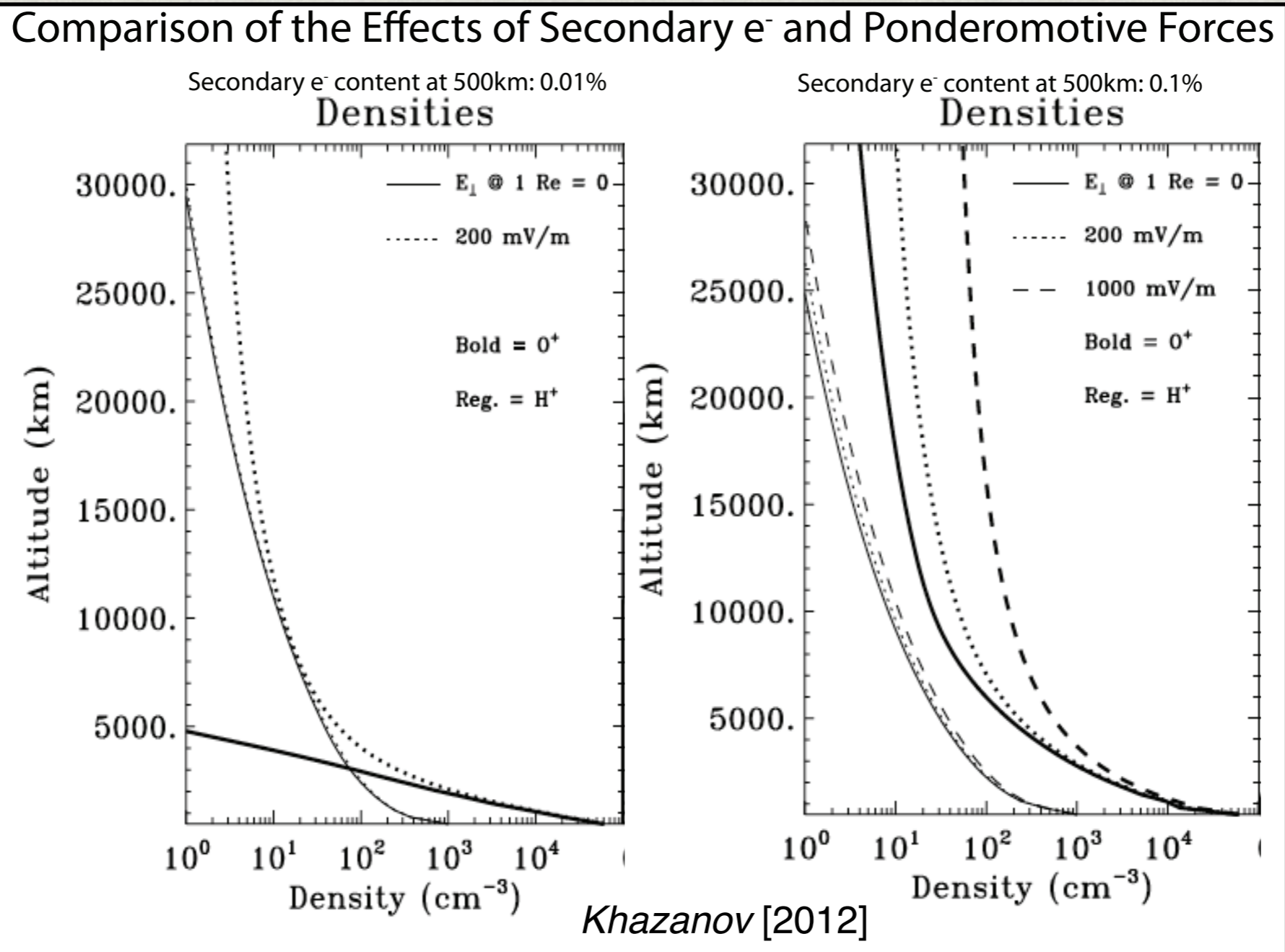


- 🌐 Studies including photoelectrons are primarily O<sup>+</sup> to high altitude as photoelectron concentration increases.
- 🌐 Secondary electrons act just as photoelectrons do.

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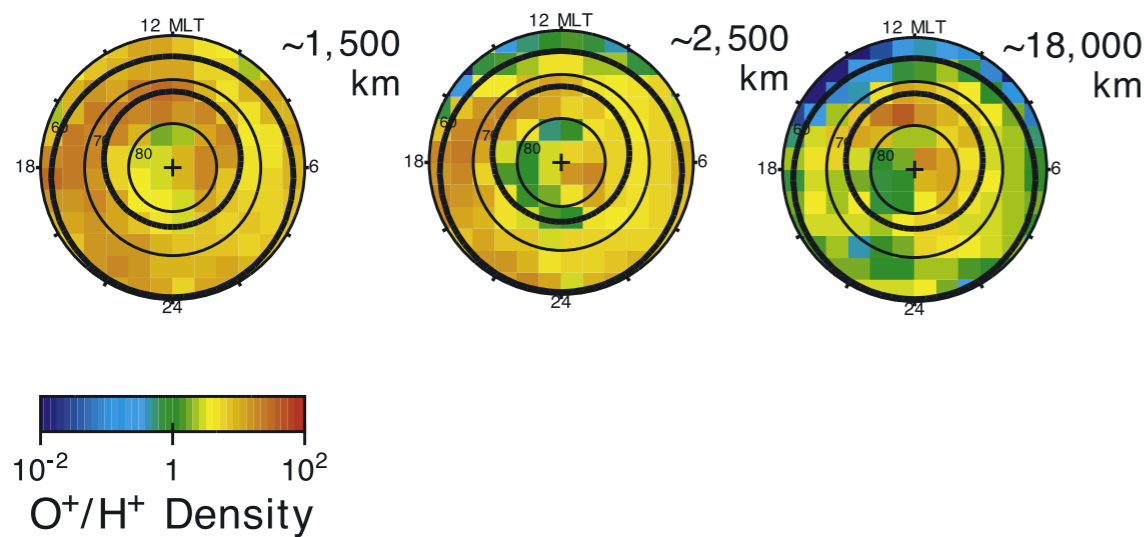
# Effect of SEs on Outflow



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# Wave-Particle Interactions in Outflow

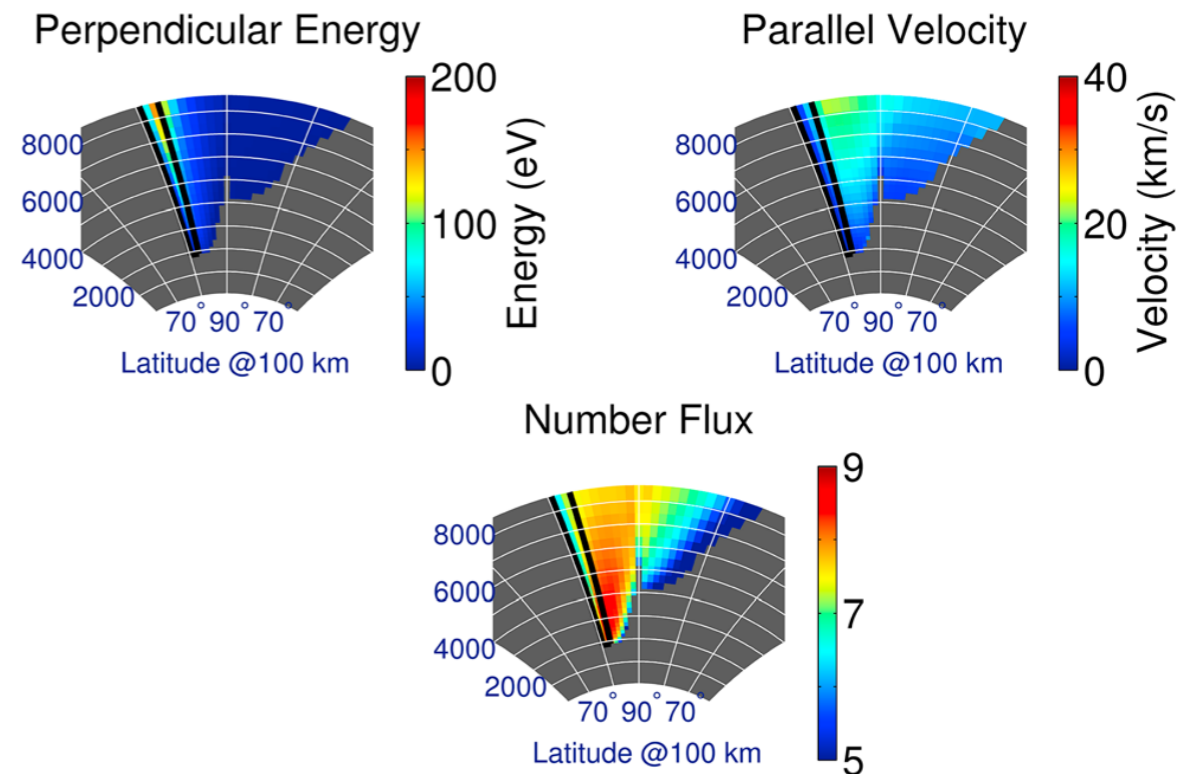
## GPW



- The solution along multiple flux tubes are followed to find the 3D solution.
- A hybrid solution with macroscopic PIC ions.
- The wave heating terms are empirical based on DE observations.

*Barakat and Schunk, [2006]*

## IPWM

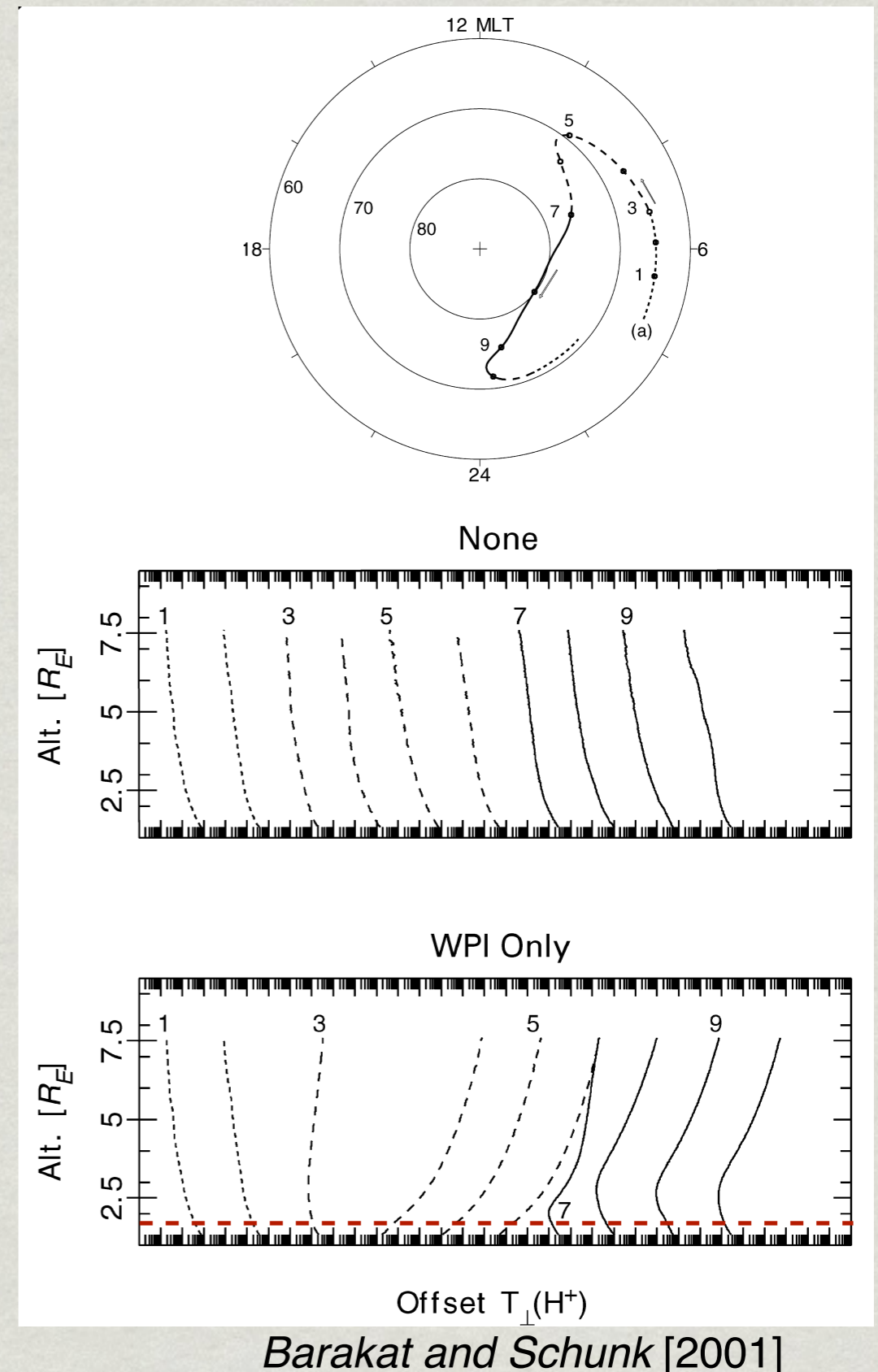


- Eight moment fluid solution for the outflow on Eulerian grid.
- A separate energized fluid is tracked to include wave heating.

*Varney et al, [2015]*

# The Missing role of Transverse Heating in Merging

- W-P interactions have a strong effect on  $T_{\perp}$ :
  - Starting at 1 $R_E$  altitude in the cusp (5).
  - Starting at 2 $R_E$  altitude in the polar cap (7).
  - In both cases the transverse heating increases with altitude.
- Heating of  $T_{\perp}$  increases the mirror force which can result in strong field aligned flows.
- Typical MHD boundaries are at 1.5 $R_E$  altitude misses a portion of the heating in the cusp.
- More importantly, MHD has an isotropic pressure which cannot account for transverse heating or the consequences.
- Current methods of merging rely entirely on the flux and completely neglect anisotropy.



# Extending MHD is Required

## Anisotropic MHD Equations

(Meng et al. [2012])

$$\frac{\partial \rho}{\partial t} + (\mathbf{u} \cdot \nabla) \rho + \rho (\nabla \cdot \mathbf{u}) = 0$$

$$\rho \frac{\partial \mathbf{u}}{\partial t} + \rho (\mathbf{u} \cdot \nabla) \mathbf{u} + \nabla (p_{\perp} + p_e) + \nabla \cdot [(p_{\parallel} - p_{\perp}) \mathbf{b}\mathbf{b}] + \frac{1}{\mu_0} \mathbf{B} \times (\nabla \times \mathbf{B}) = 0$$

Mirror-like force, converts random perpendicular motion to organized parallel motion

$$\frac{\partial \mathbf{B}}{\partial t} + \nabla \times [-(\mathbf{u} \times \mathbf{B})] = 0$$

$$\frac{\partial p_{\parallel}}{\partial t} + (\mathbf{u} \cdot \nabla) p_{\parallel} + p_{\parallel} (\nabla \cdot \mathbf{u}) + 2p_{\parallel} \mathbf{b} \cdot (\mathbf{b} \cdot \nabla) \mathbf{u} = 0$$

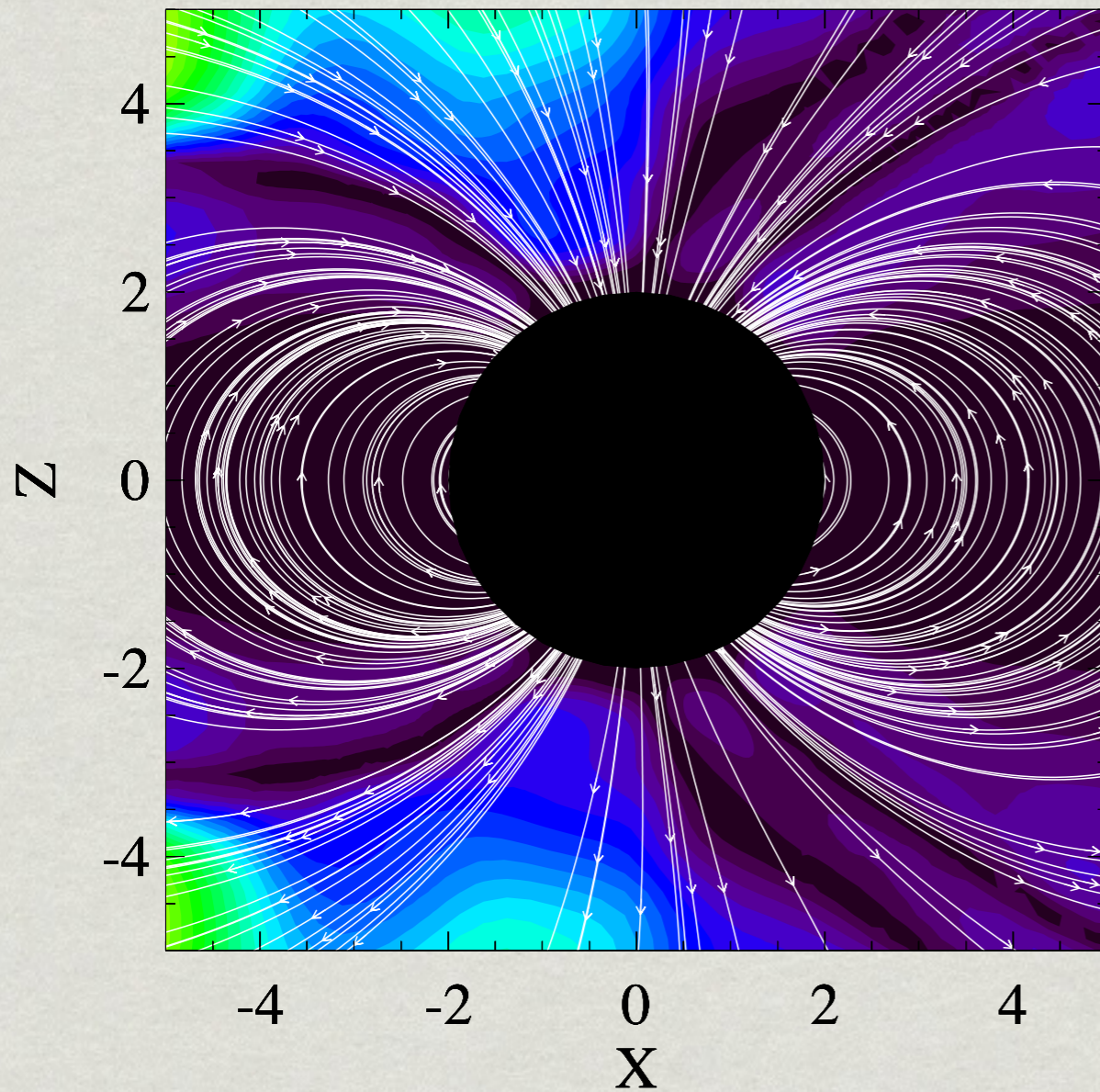
$$\frac{\partial p_{\perp}}{\partial t} + (\mathbf{u} \cdot \nabla) p_{\perp} + 2p_{\perp} (\nabla \cdot \mathbf{u}) - p_{\perp} \mathbf{b} \cdot (\mathbf{b} \cdot \nabla) \mathbf{u} = 0 + \langle \delta P_{\perp} / \delta t \rangle_{\text{waves}}$$

$$\frac{\partial p_e}{\partial t} + (\mathbf{u} \cdot \nabla) p_e + \frac{5}{3} p_e (\nabla \cdot \mathbf{u}) = 0$$

# Effect of WPI on Velocity

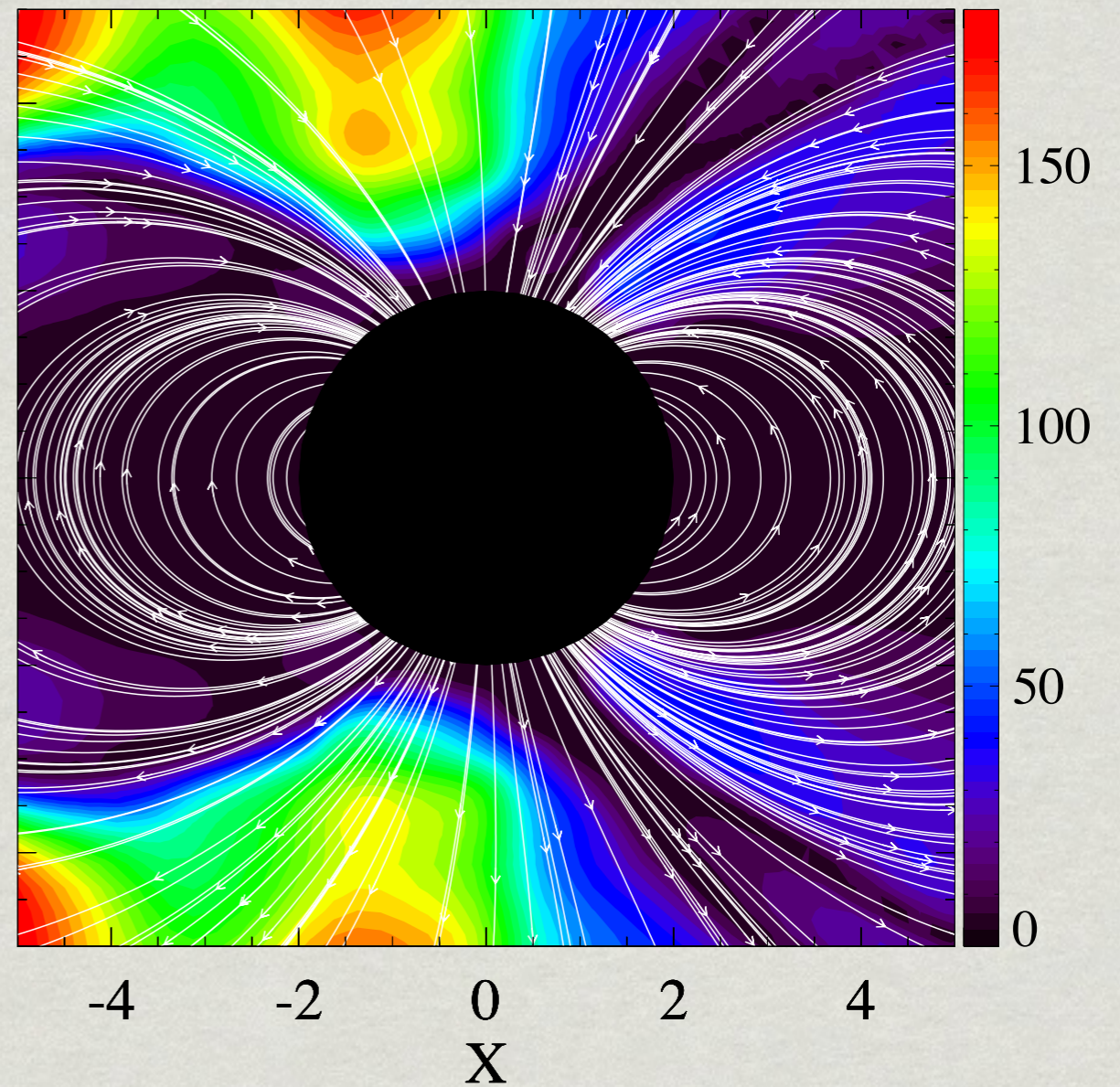
No WPI Source Term

Field-Aligned Velocity



With WPI Source Term

Field-Aligned Velocity





# Including The Ring Current

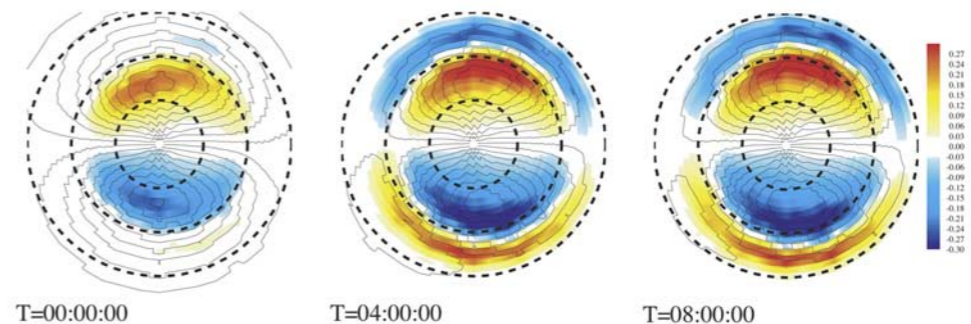
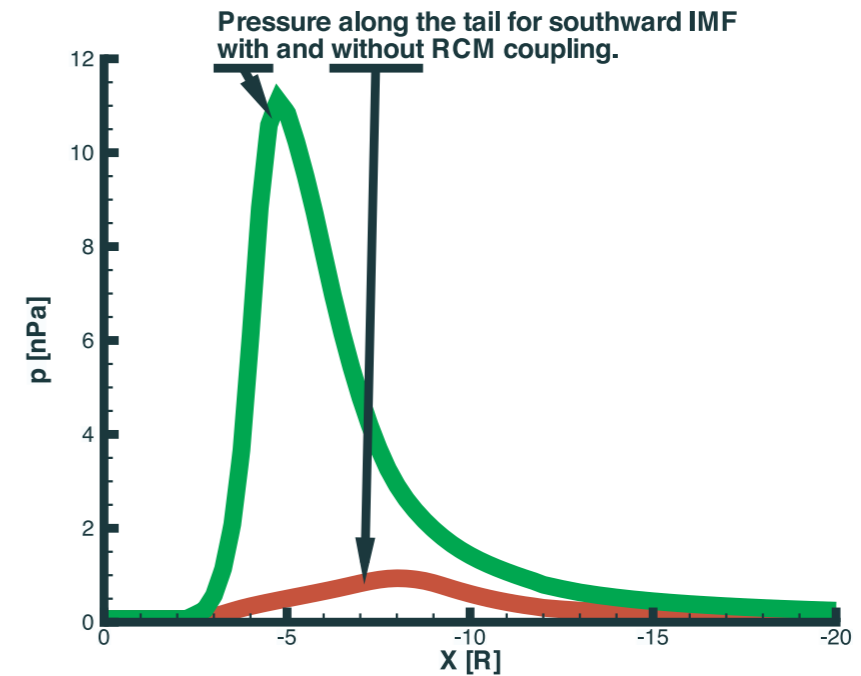
- Global MHD models do not include the drift physics required to capture the ring current.
- Putting the two approaches together yields advantages for each.
- For the global MHD model:
  - Improved representation of the inner magnetospheric pressure.
  - Better region 2 currents.
  - More accurate and consistent representation of the magnetic field.
- For the ring current model:
  - More accurate, consistent, representation of the magnetic and electric fields
  - Dynamic and MLT dependent boundary

# Coupling RCM and BATS-R-US

$$\frac{\partial \eta_s}{\partial t} + \frac{\mathbf{B} \times \nabla \left( \Phi + \Phi_c + \frac{\lambda_s}{q_s} V^{-2/3} \right)}{B^2} \cdot \nabla \eta_s = -L.$$

$$\lambda_s = W_s V^{2/3} \quad \eta_s = n_s V$$

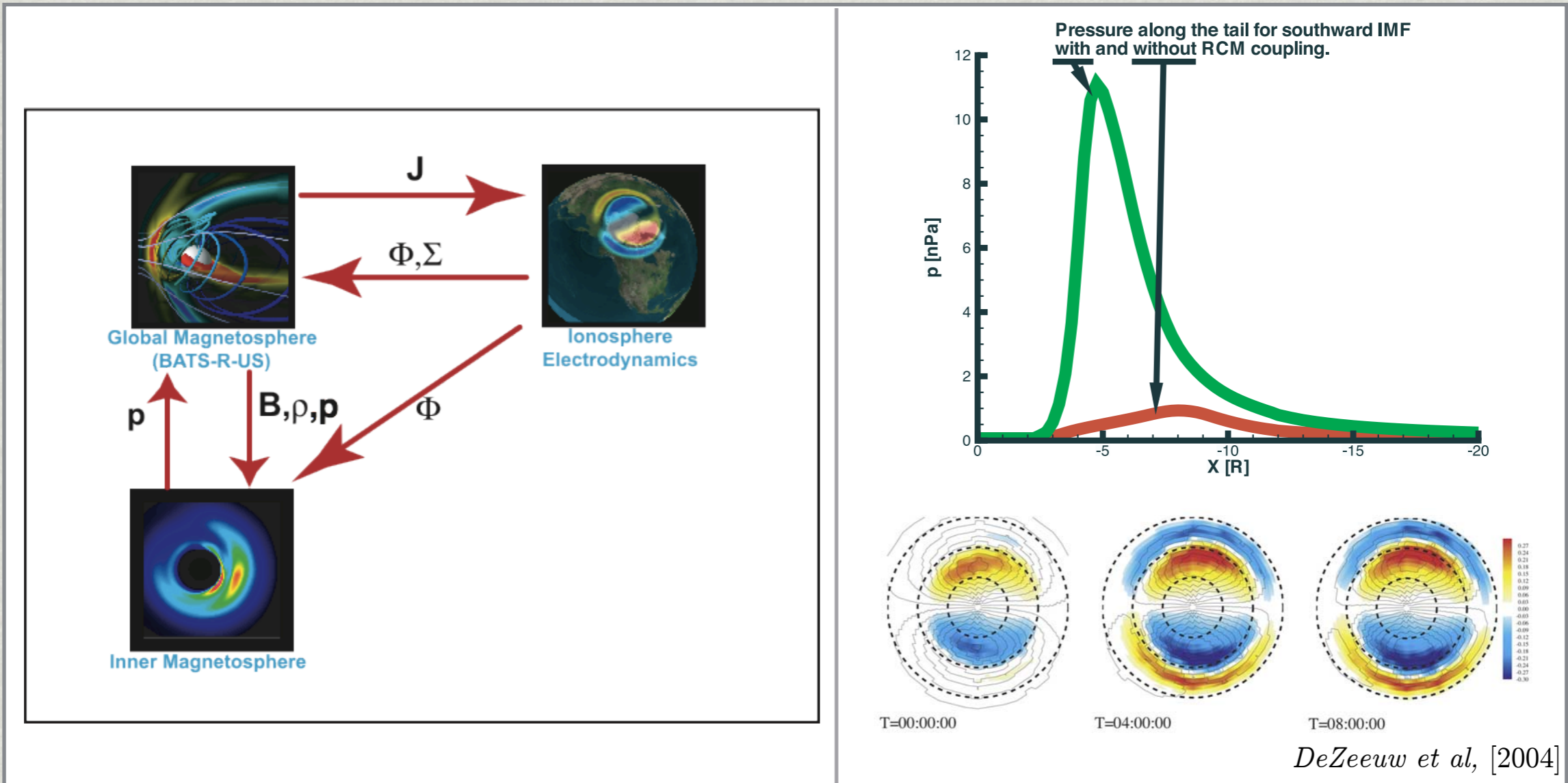
*Wolf, [1983]*



*DeZeeuw et al, [2004]*

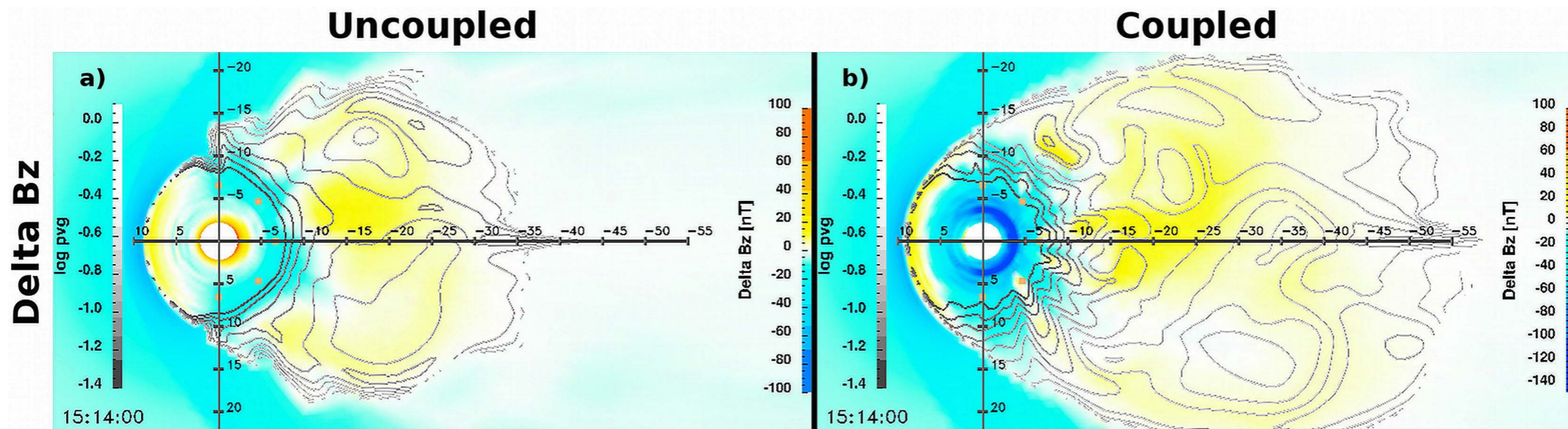
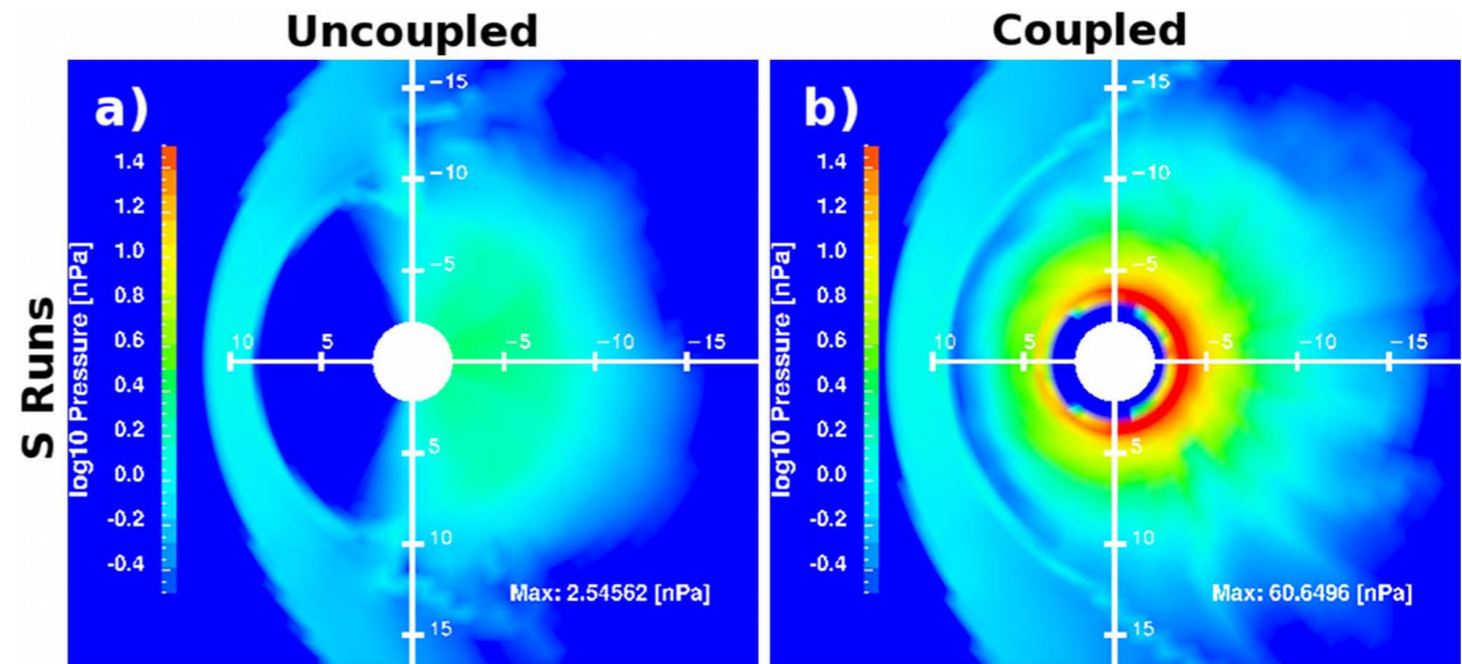
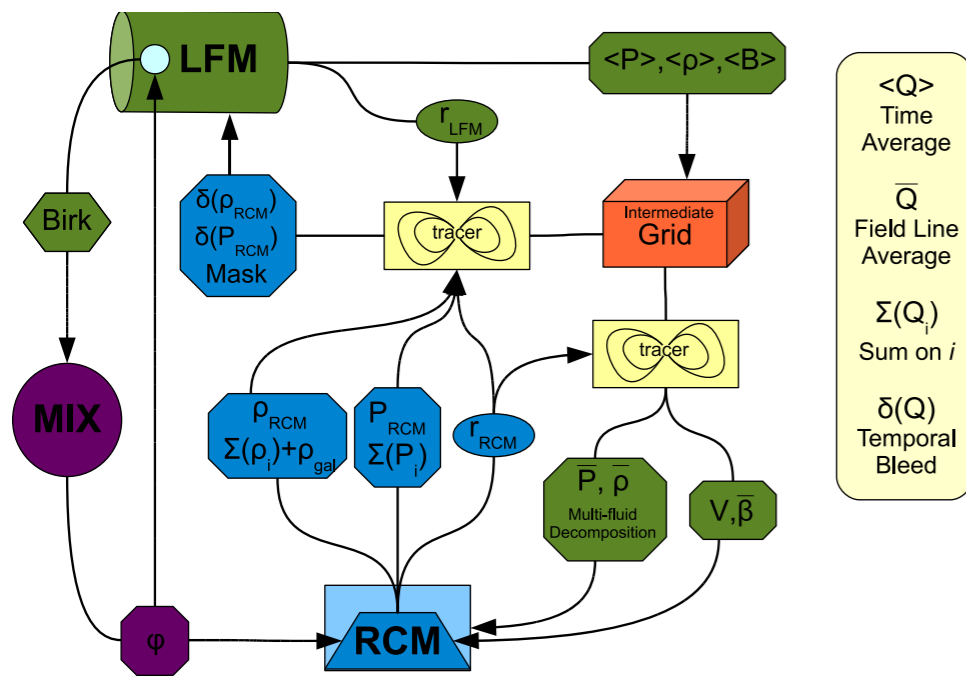
- First coupling of ring current model to MHD
- Advantages: Ring current drift and pressure effects now represented in global magnetosphere model.
- Disadvantage: Only isotropic ring current distributions distributions.

# Coupling RCM and BATS-R-US

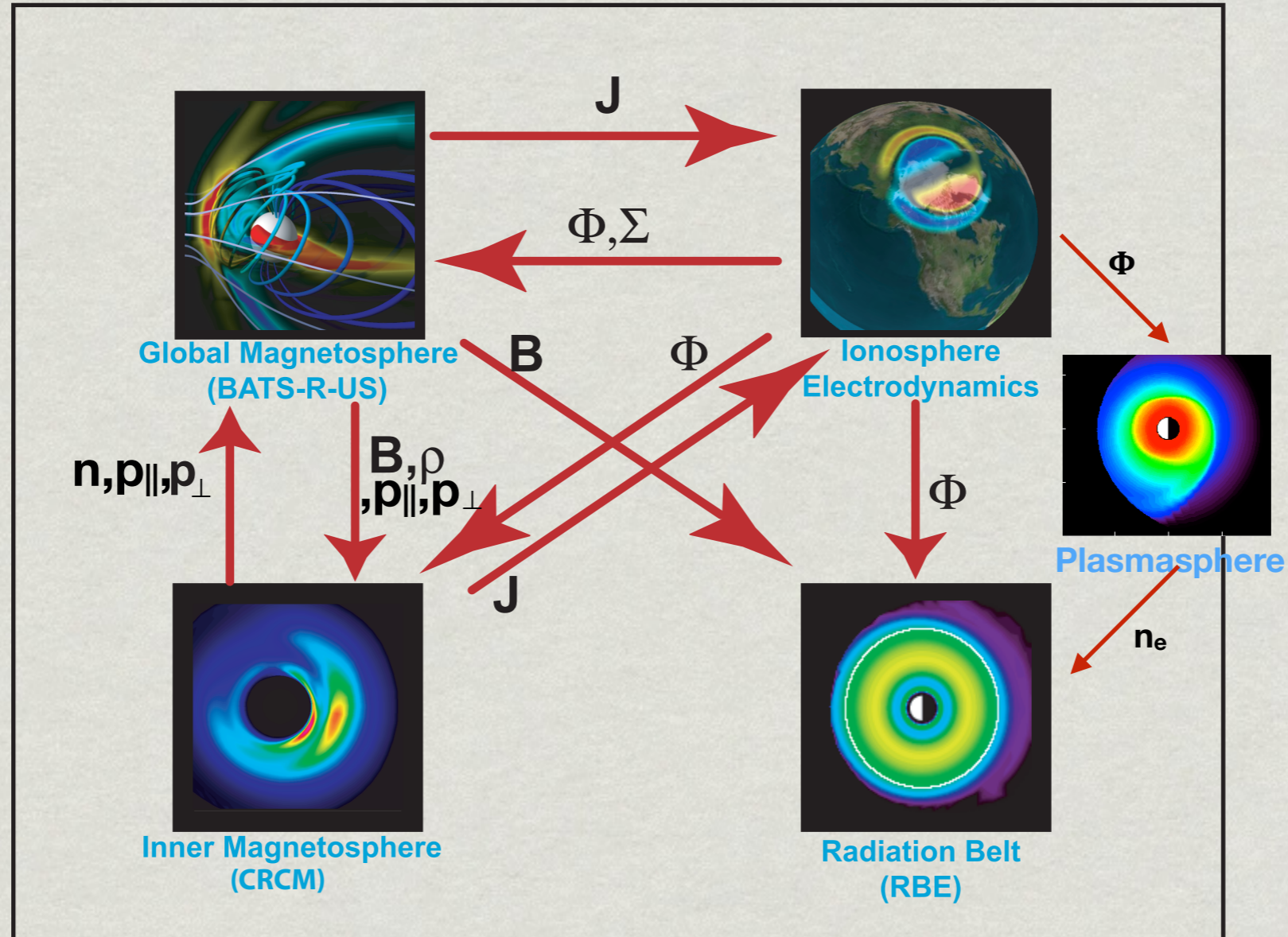


- First coupling of ring current model to MHD
- Advantages: Ring current drift and pressure effects now represented in global magnetosphere model.
- Disadvantage: Only isotropic ring current distributions distributions.

# Coupling RCM and LFM-MIX

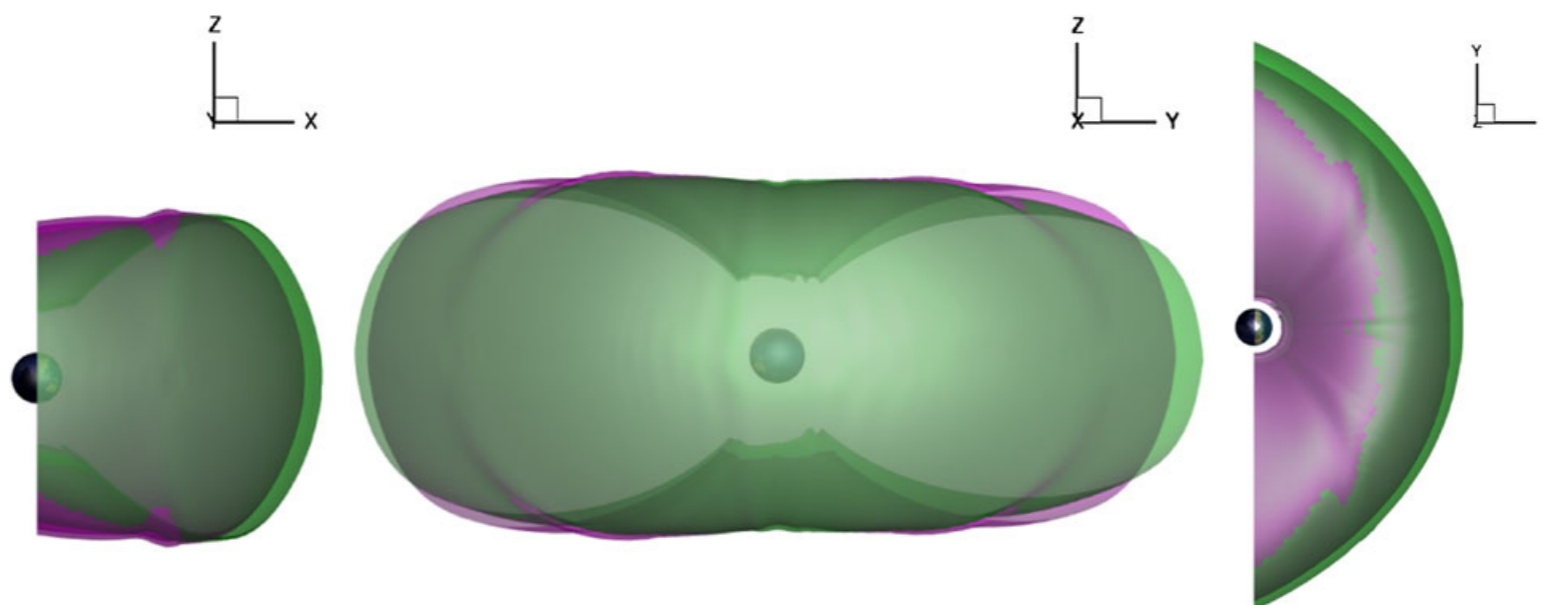
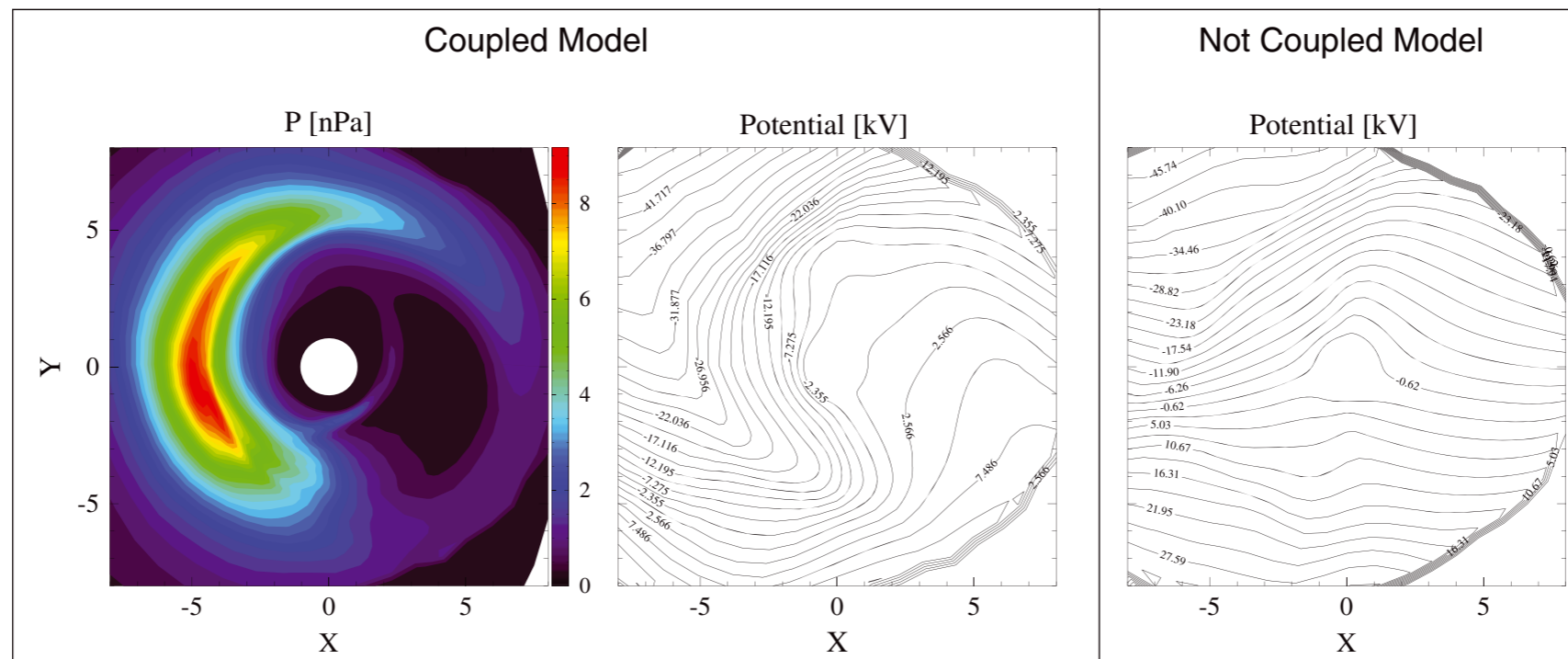


# Description of Existing Model Couplings



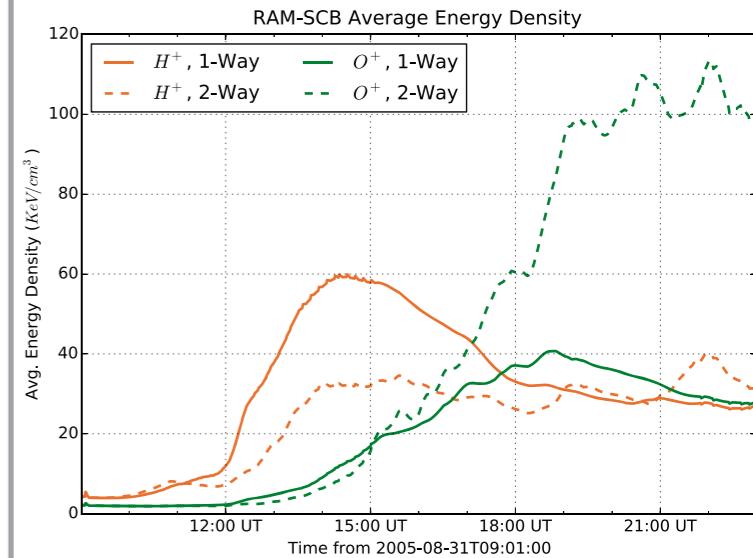
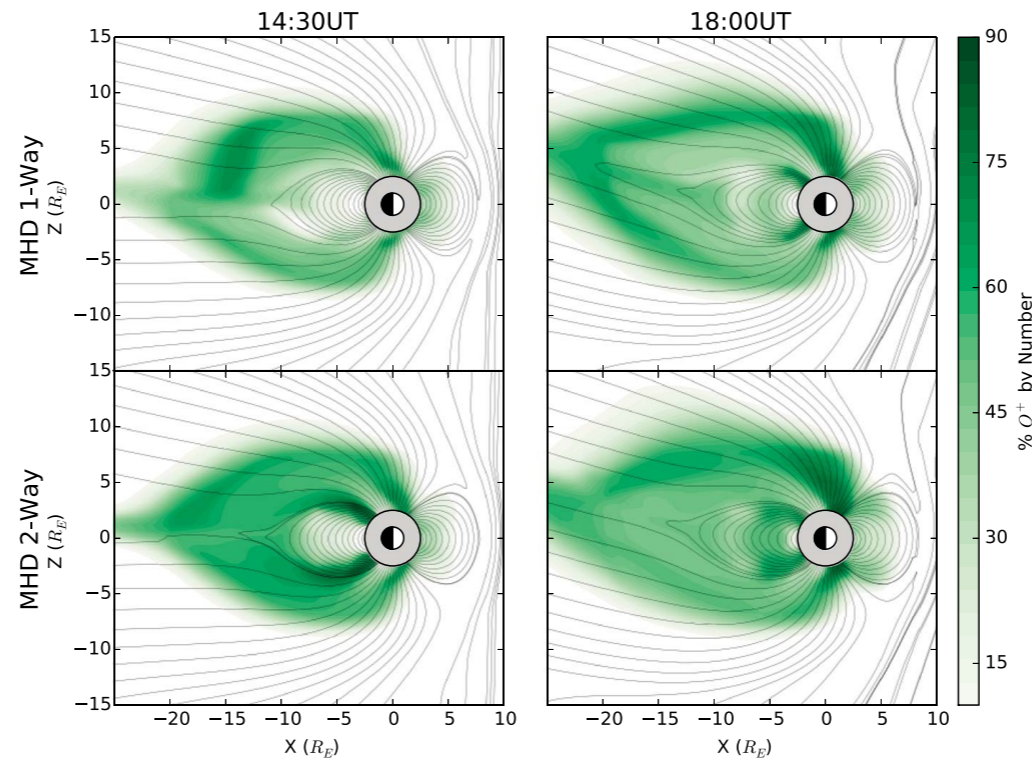
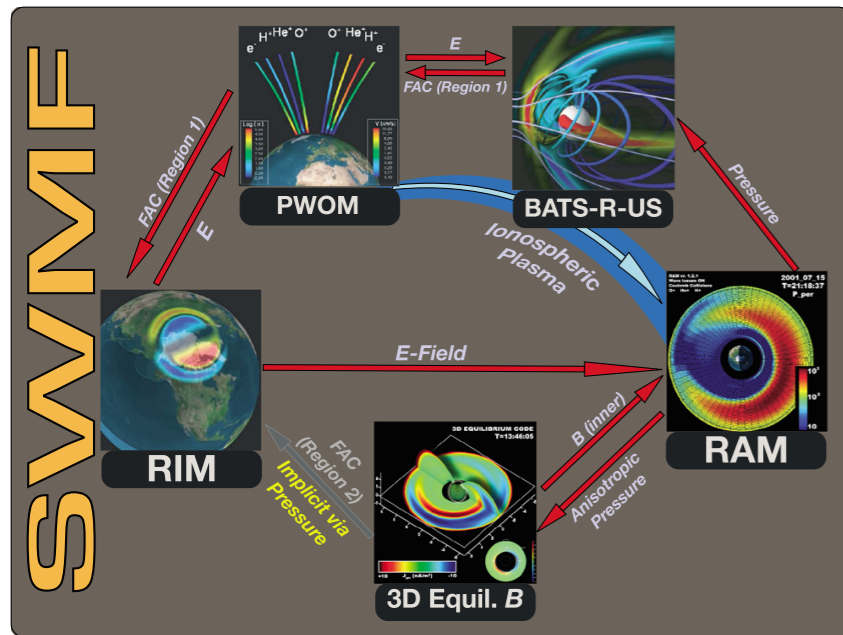
- 🌐 Glocer, A., G. Toth, M. Fok, T. Gombosi, M. Liemohn (2009), Integration of the radiation belt environment model into the space weather modeling framework, *Journal of Atmospheric and Solar-Terrestrial Physics*, doi:10.1016/j.jastp.2009.01.003.
- 🌐 Glocer, A., M. Fok, X. Meng, G. Toth, N. Buzulukova, S. Chen, and K. Lin (2013), CRCM + BATS-R-US two-way coupling, *J. Geophys. Res. Space Physics*, 118, 1635–1650, doi:10.1002/jgra.50221.
- 🌐 Meng, X., G. Tóth, A. Glocer, M.-C. Fok, and T. I. Gombosi (2013), Pressure anisotropy in global magnetospheric simulations: Coupling with ring current models, *J. Geophys. Res. Space Physics*, 118, 5639–5658, doi:10.1002/jgra.50539.

# Coupling RC models change E and B fields



*Gloer et al, [2013]*

# Coupling RAM-SCB and BATS-R-US

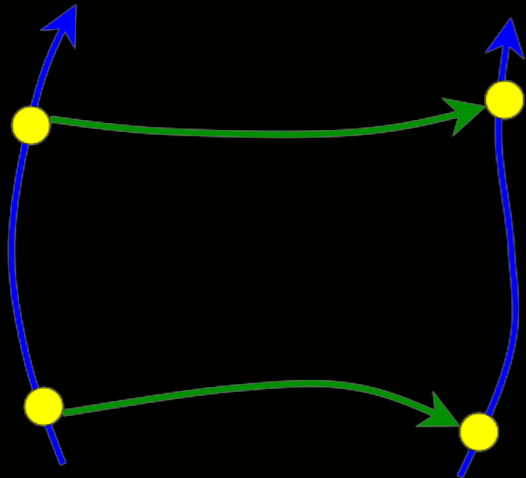


Welling et al, [2015]

- Welling et al., 2015 use the coupled RAM-SCB code to explore effect of including ring current feedback on the ionospheric source.
- Including ring current effects in the global model feedback to the outflow source and ultimately back to the ring current.

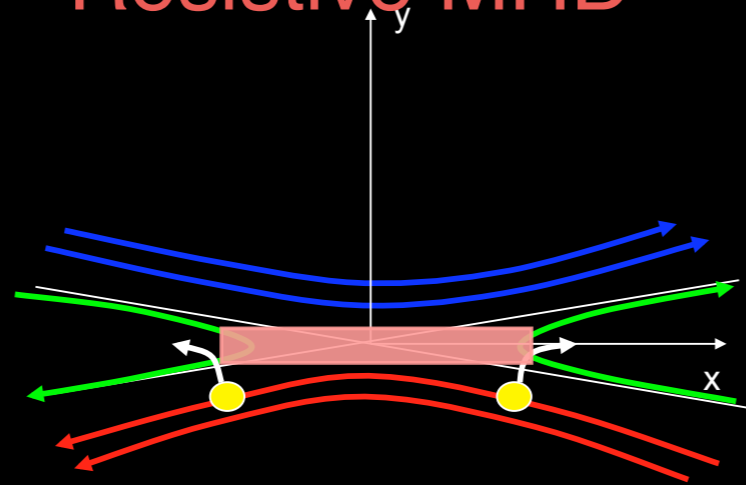
# Reconnection and Global Modeling

Ideal MHD



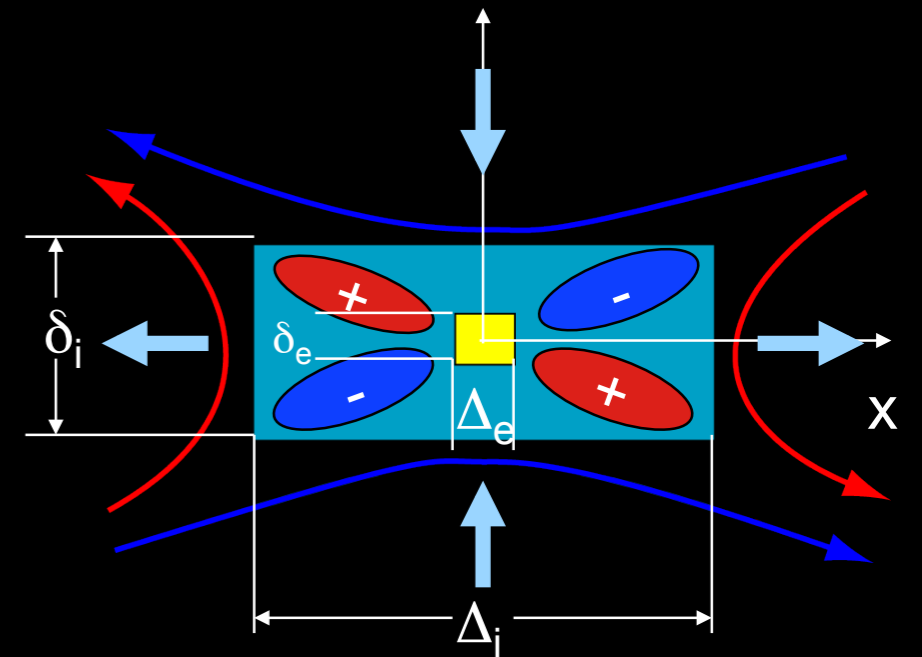
$$E = -\frac{1}{c}U \times B$$

Resistive MHD



$$+ \eta \mathbf{J}$$

Hall MHD

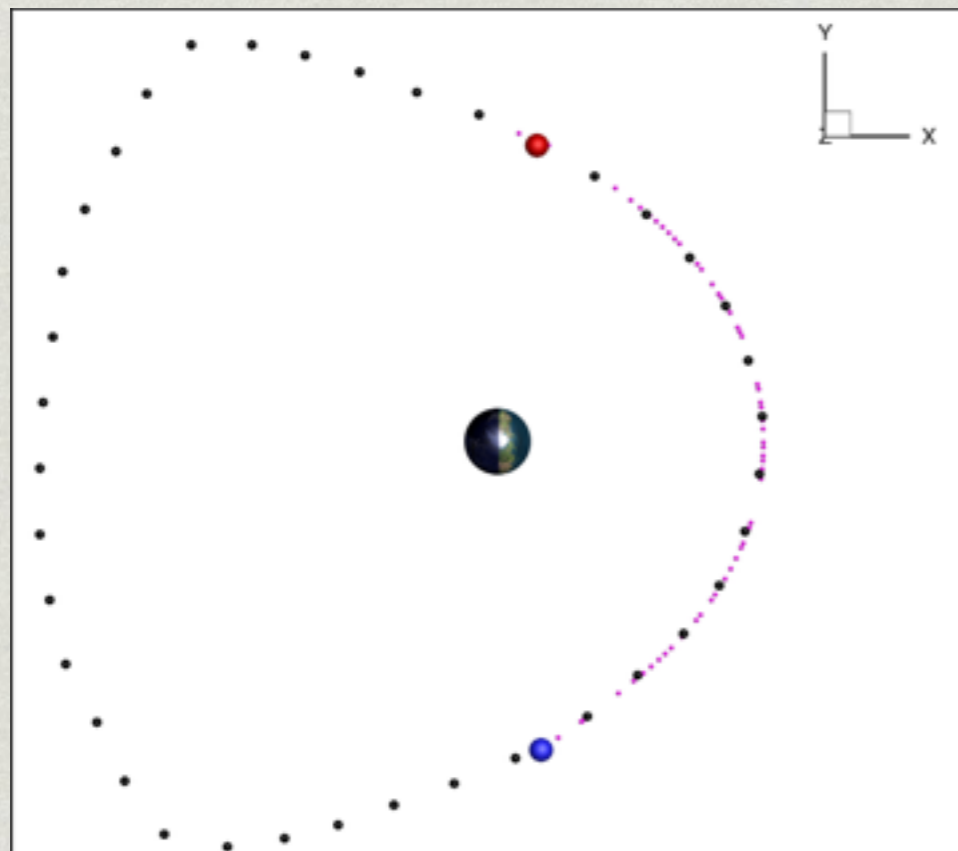
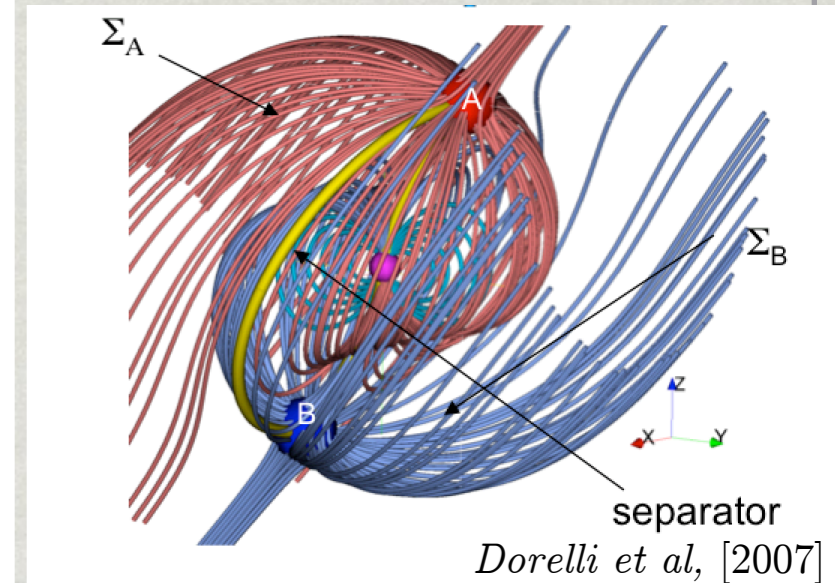
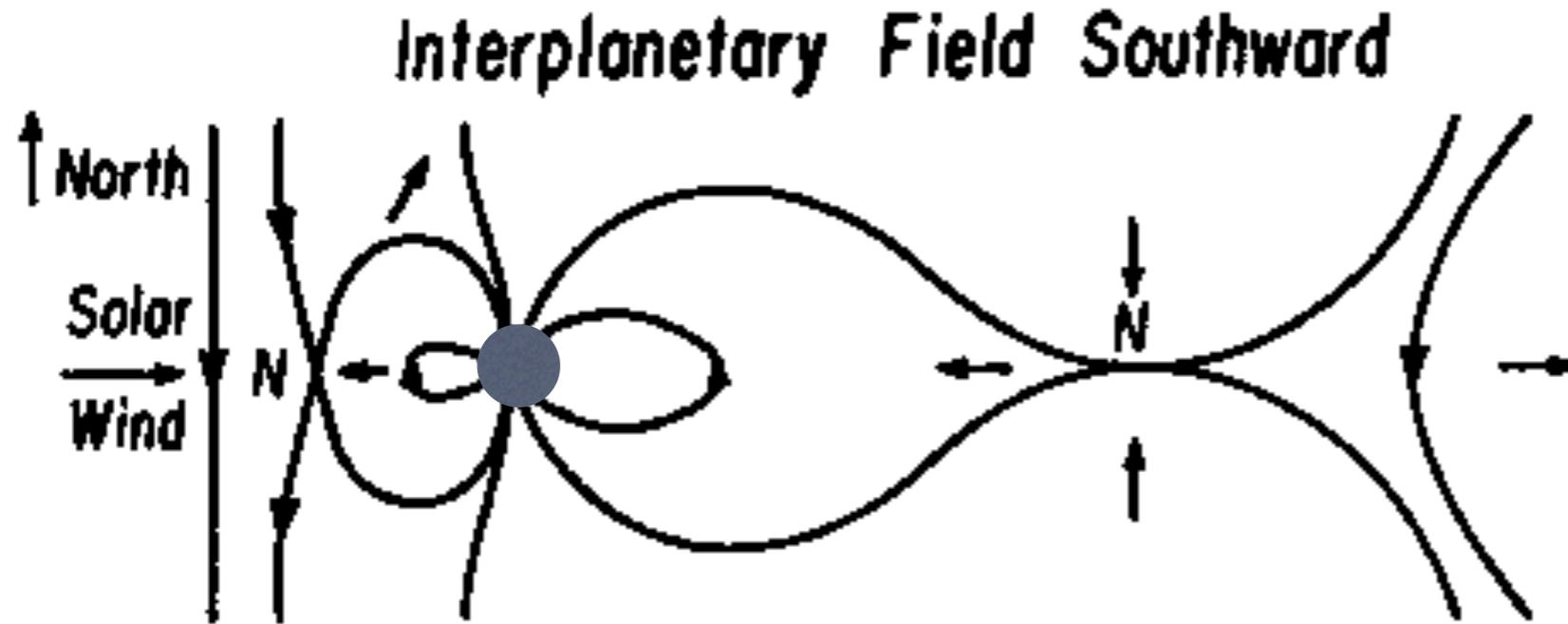


$$+ \frac{1}{nec} \mathbf{J} \times \mathbf{B} - \frac{1}{ne} \nabla \cdot \mathbf{p}_e^{CM}$$

- Most global magnetosphere models are solving resistive MHD equations with either physical or numerical resistivity.
- We are starting to see more extensions to Hall MHD



# What is a Magnetic Separator?

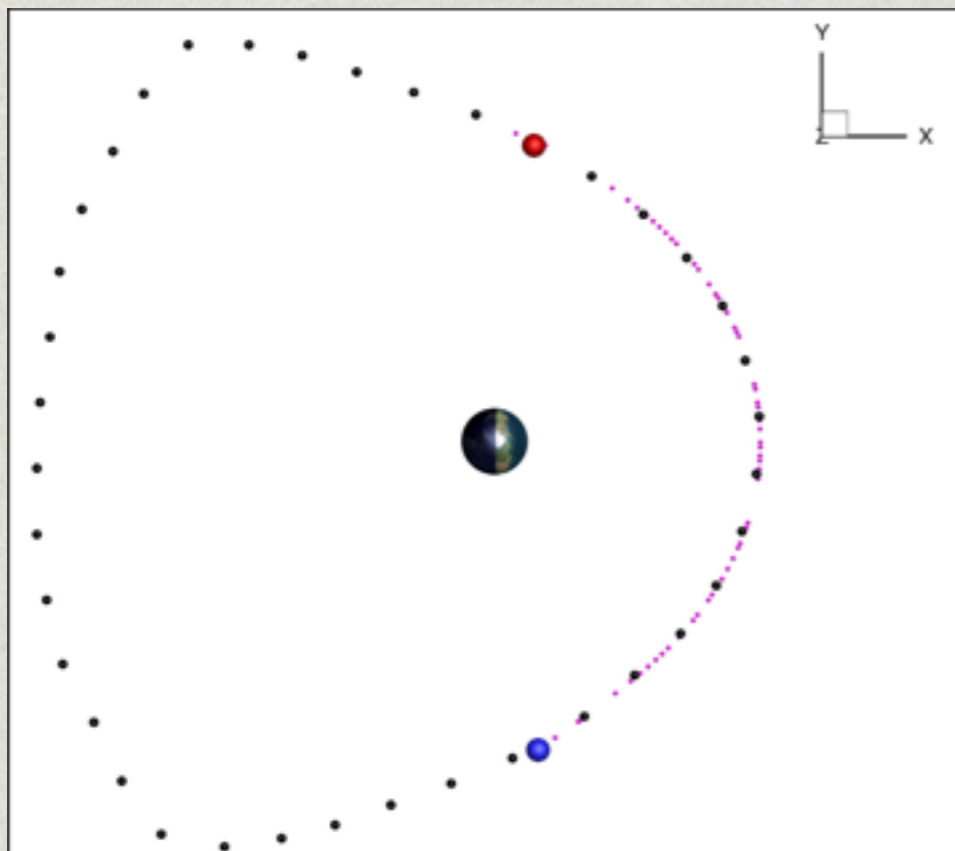
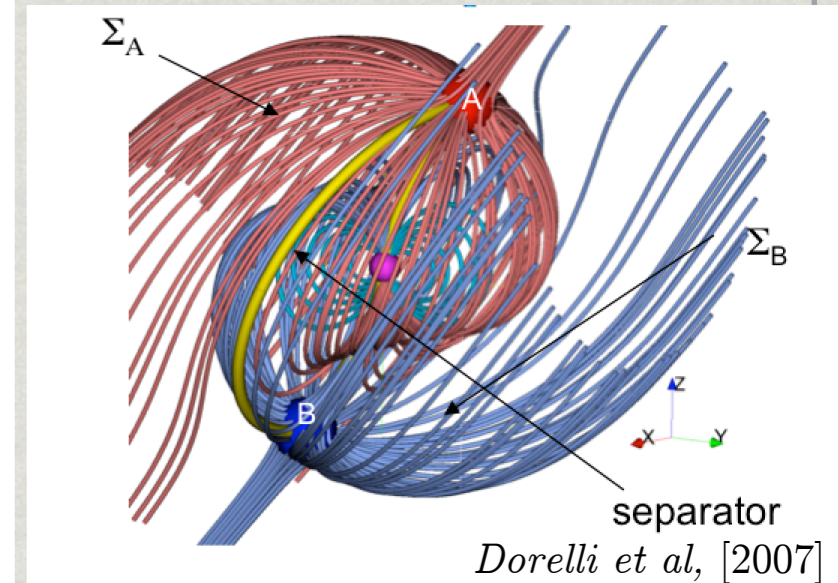
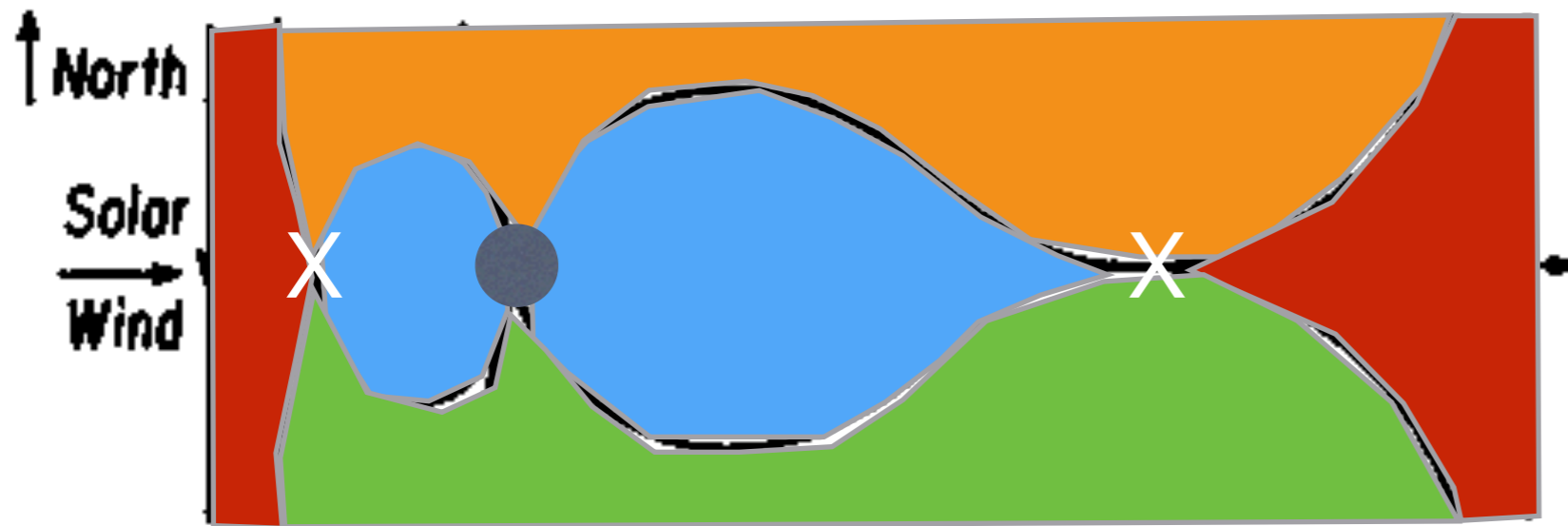


$$\frac{d\Phi_B}{dt} = \oint E_{\parallel} ds = \int_{DS} E_{\parallel} ds + \int_{NS} E_{\parallel} ds$$

- For further reading about separators see:
  - Lau and Finn, [1990]
  - Sisco et al., [2001]
  - Dorelli et al., [2007]...

# What is a Magnetic Separator?

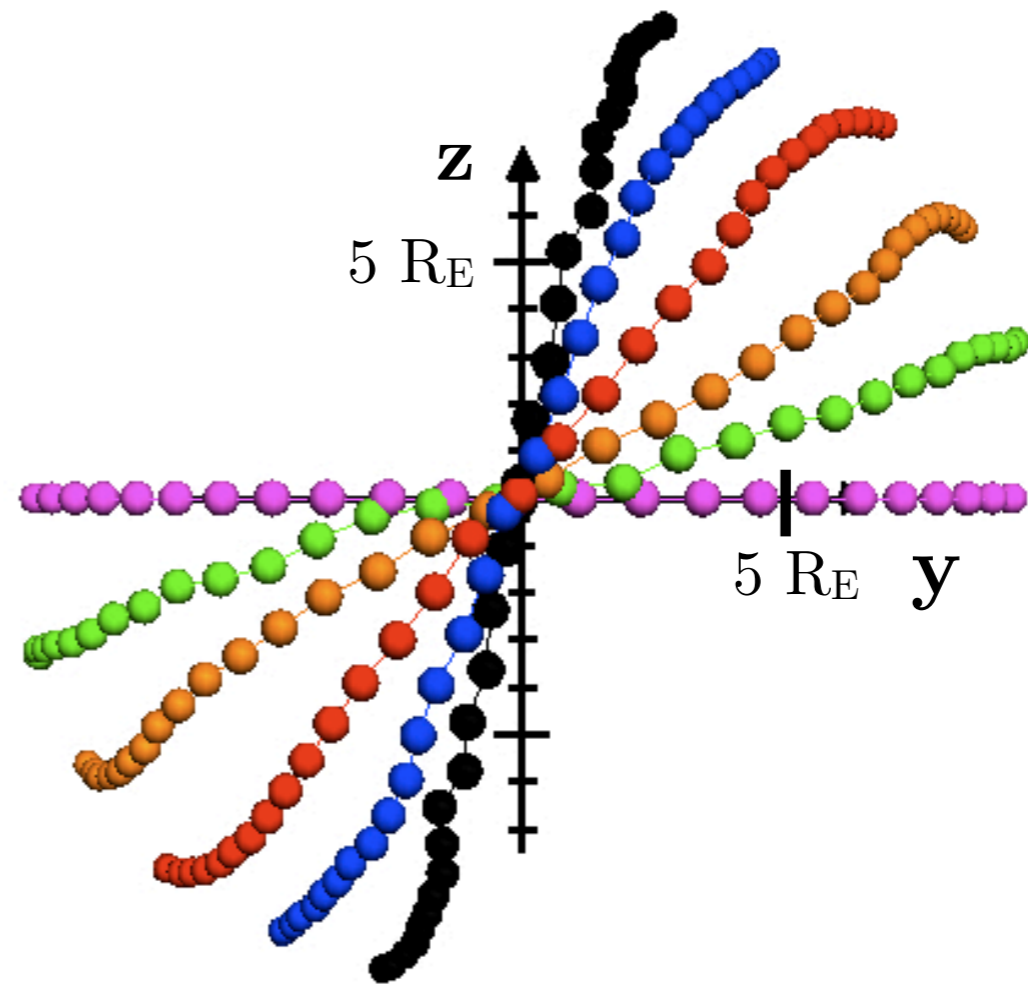
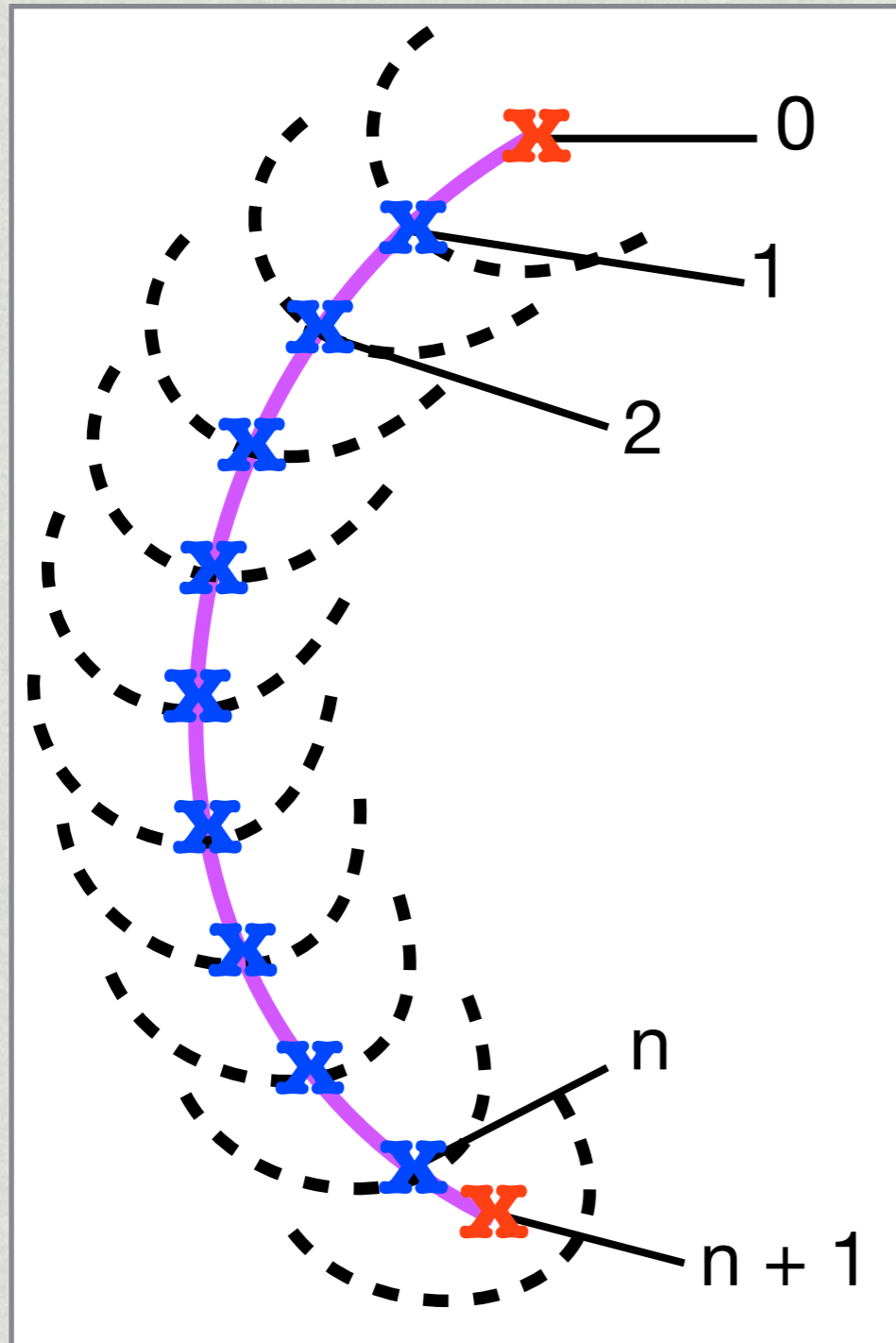
## Interplanetary Field Southward



$$\frac{d\Phi_B}{dt} = \oint E_{\parallel} ds = \int_{DS} E_{\parallel} ds + \int_{NS} E_{\parallel} ds$$

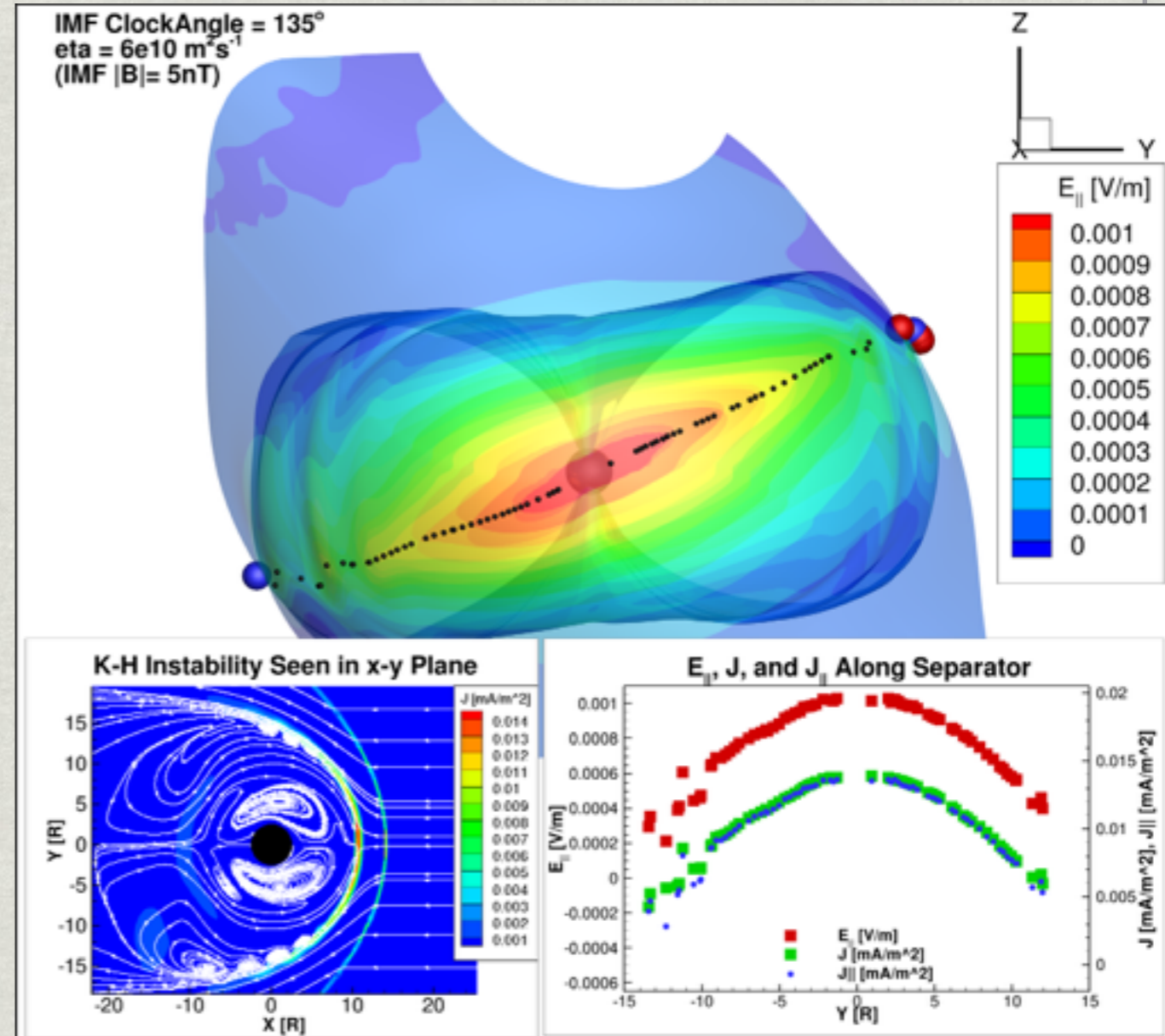
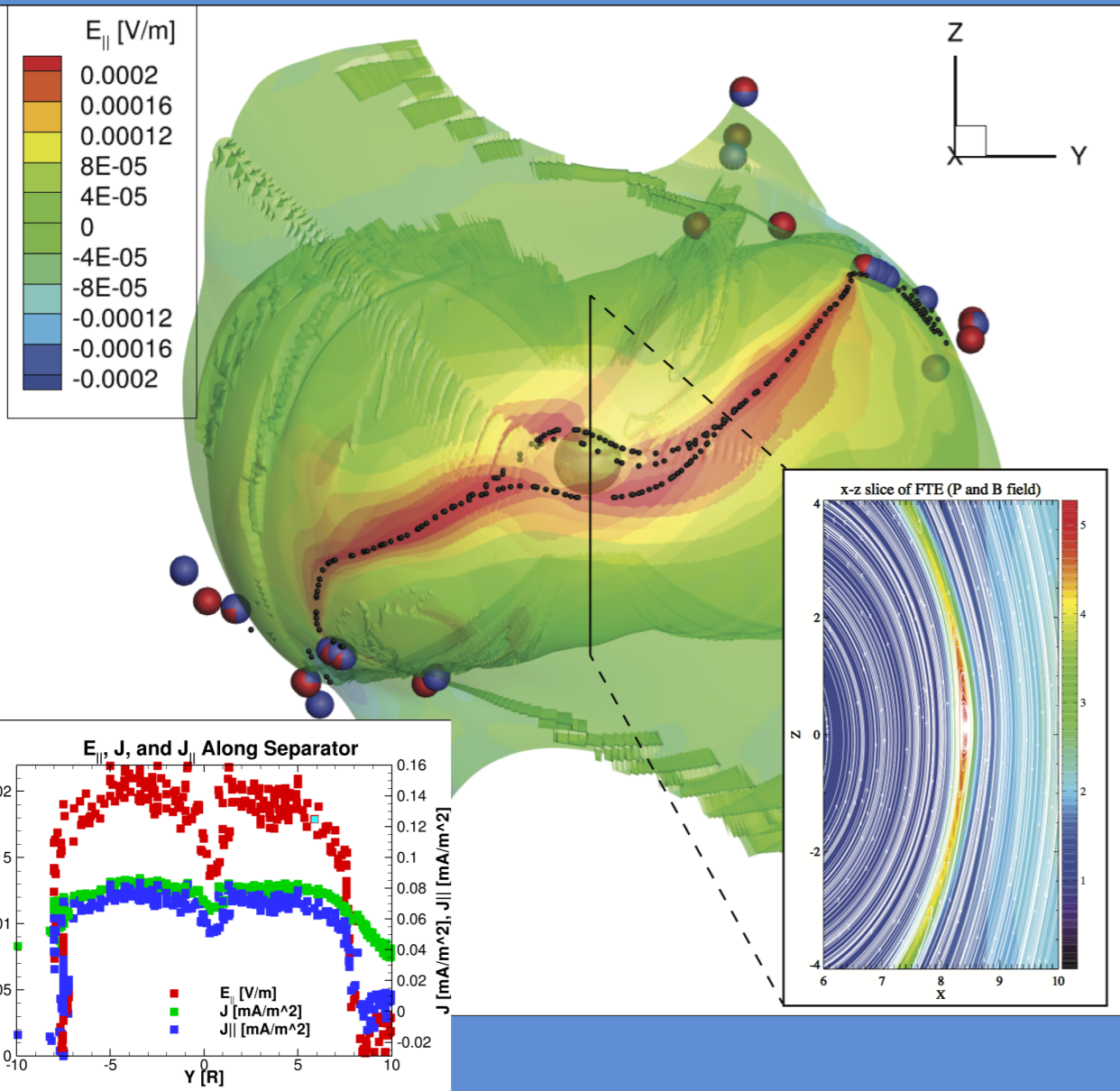
- For further reading about separators see:
  - Lau and Finn, [1990]
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  - Dorelli et al., [2007]...

# Locating Separators



*Komar et al, [2013]*

# Separators for more complex cases



# Generalized Ohm's Law

$$E = -\frac{1}{c}U \times B + \underbrace{\sum_{\alpha} \int dv q_{\alpha} n_{\alpha} v \left( \frac{\partial f_{\alpha}}{\partial t} \right)}_{\eta J} + \frac{1}{nec} J \times B - \frac{1}{ne} \nabla \cdot P_e^{CM} - \frac{m_e}{ne^2} \frac{\partial J}{\partial t} - \frac{m_e}{ne^2} \nabla \cdot (UJ + JU)$$

Ideal MHD term (Frozen Flux Theorem)

Hall term (Electron Frozen Flux Theorem) [ION INERTIAL SCALE]

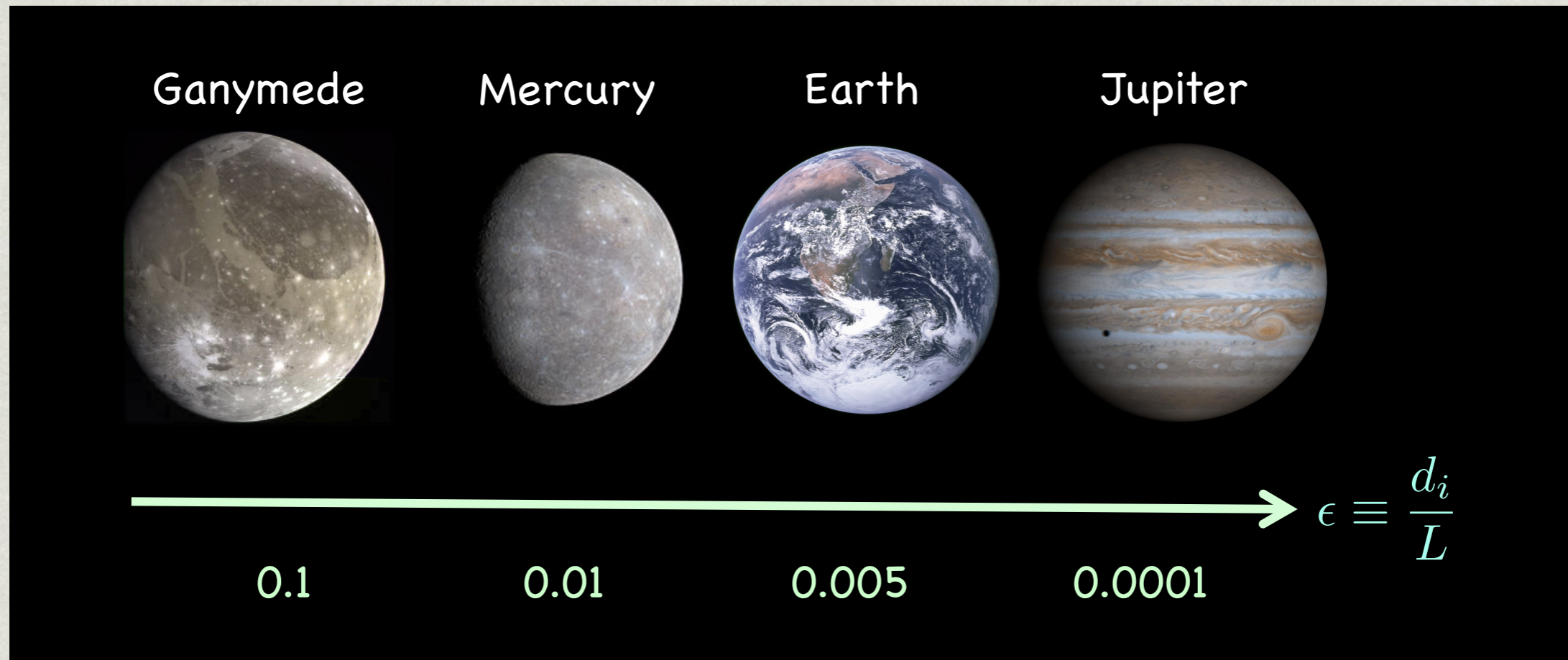
Electron Pressure Anisotropy (thaws magnetic flux) [ION INERTIAL SCALE]

Electron Inertia (thaws magnetic flux) [ELECTRON INERTIAL SCALE]

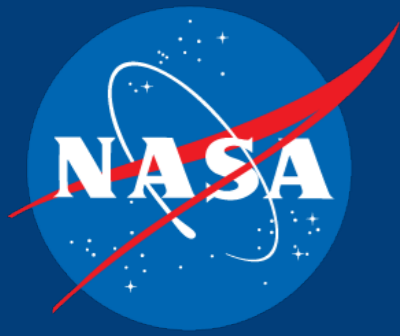
Particle Scattering (thaws magnetic flux - e.g., resistivity)

- Assuming quasineutrality and neglecting terms  $\sim m_e/m_i$  gives the above expression for the electric field.
- Each color represents a different regime.
- The results on previous slide are for resistive MHD

# Comparative Magnetospheres



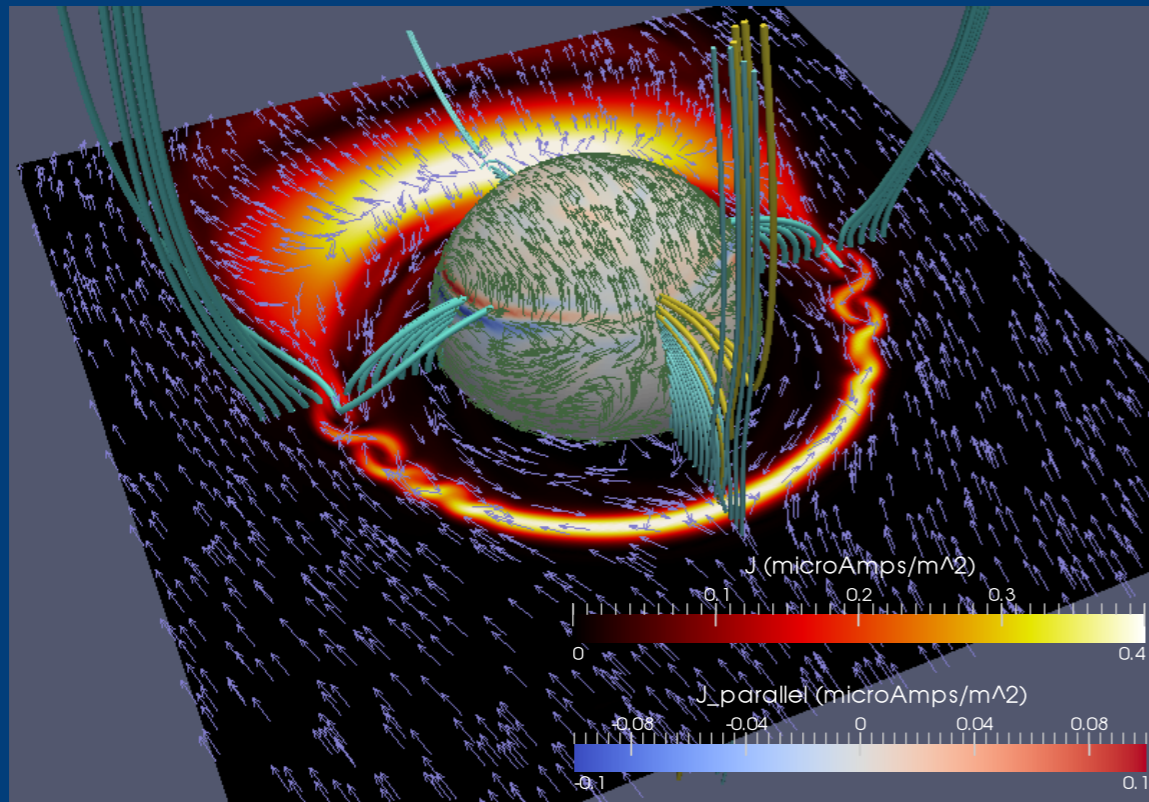
- To resolve ion scale effects you need to separate the ion scale from the diffusive scale.
- Relying on numerical resistivity would require 5-10 points per  $d_i$
- Uniformly resolving the magnetopause at this level would require billions of cells.
- The situation improves when looking at planetary magnetospheres



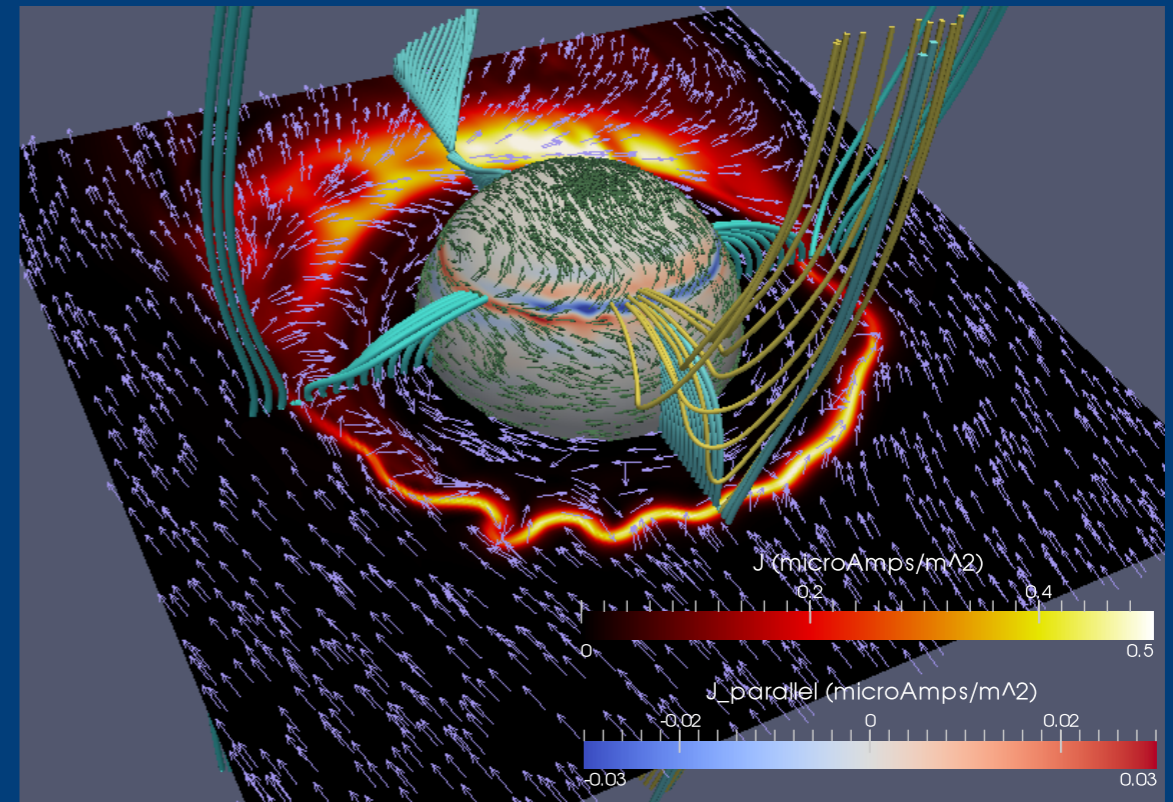
# Implications of ion-scale physics



(See Dorelli et al., 2015)



**MHD**

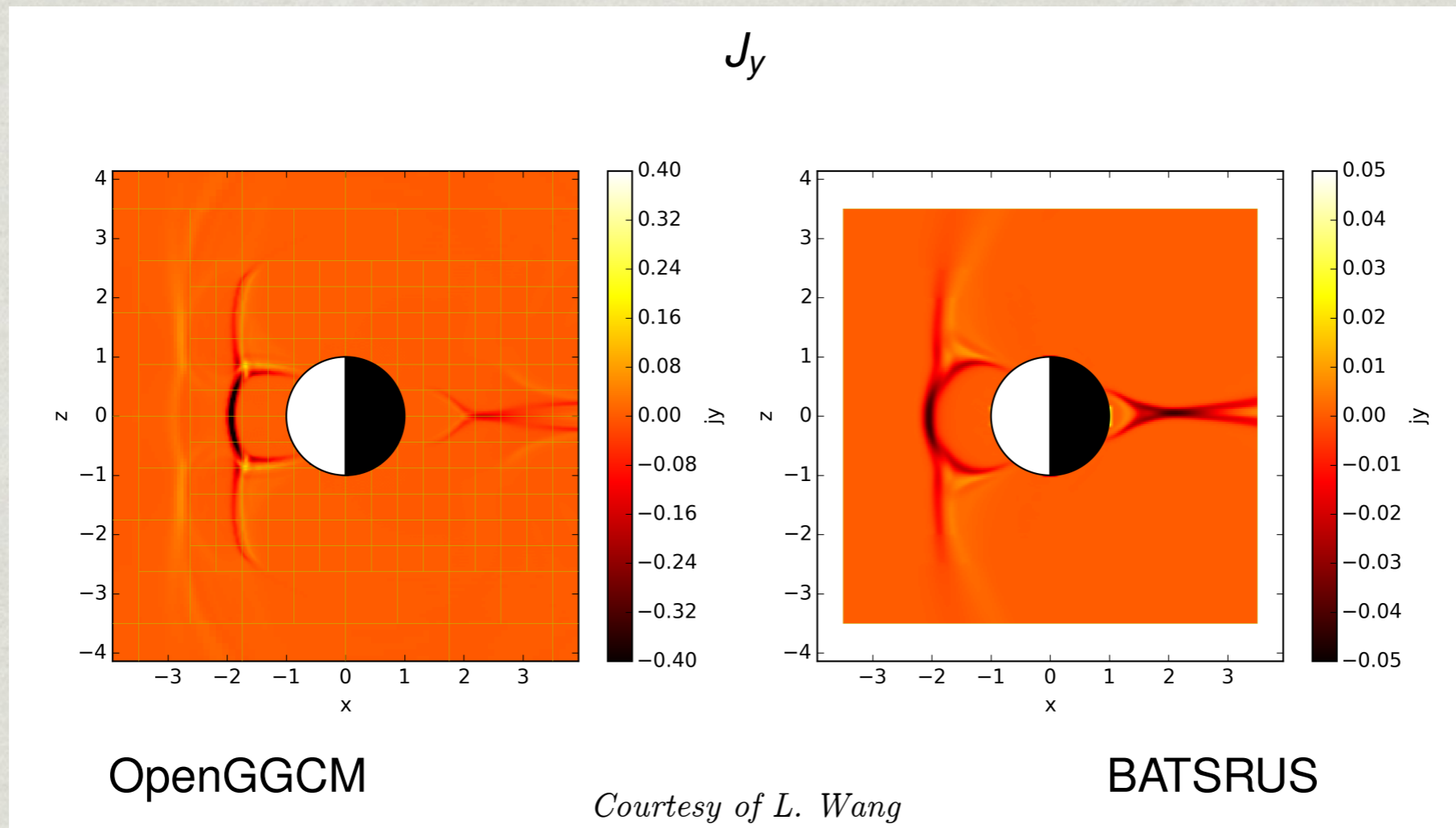


**Hall MHD**

- **symmetric Dungey convection pattern**
- **typical region-1 field-aligned current pattern (supports Alfvén wing structure)**
- **symmetric pattern of Kelvin-Helmholtz waves**

- **strong asymmetries in convection pattern**
- **new reconnection-generated field-aligned current pattern (impact on Alfvén wing structure?)**
- **Asymmetric pattern of Kelvin-Helmholtz waves**

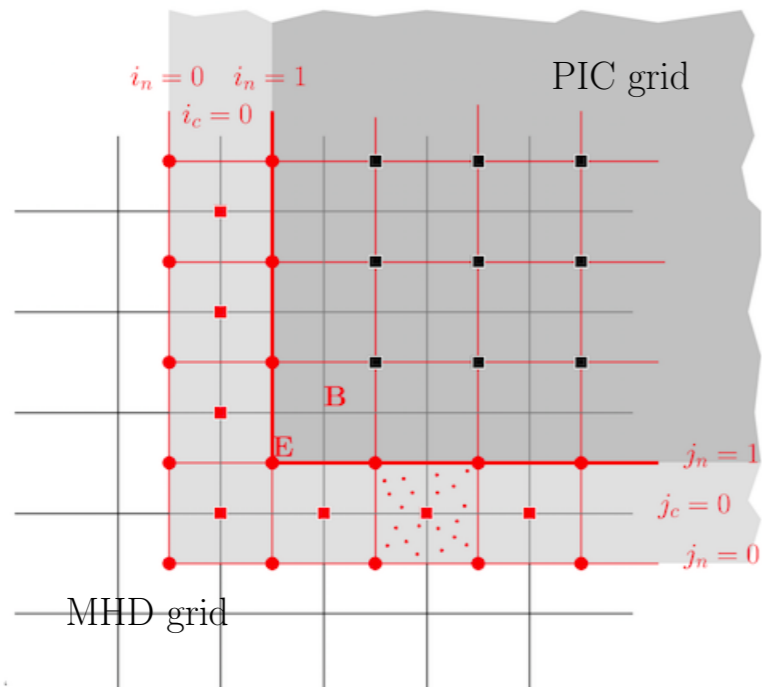
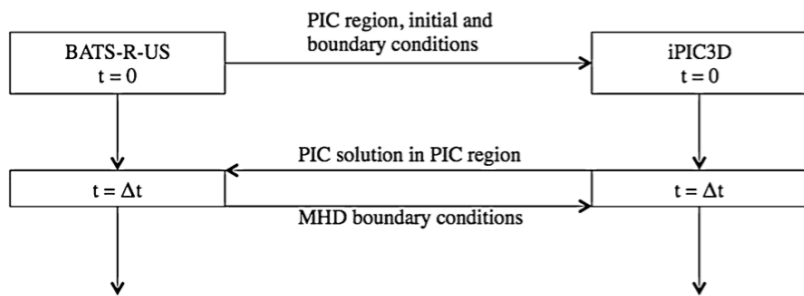
# Similar results for Ganymede for Different Models



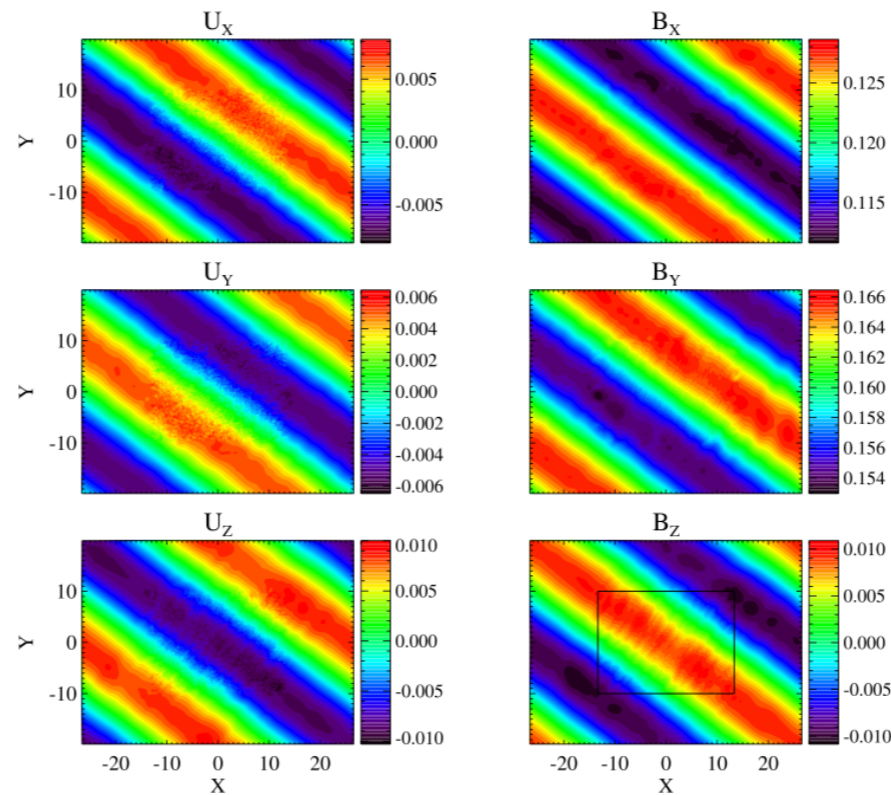


# Using EPIC-MHD

## Embedding Algorithm

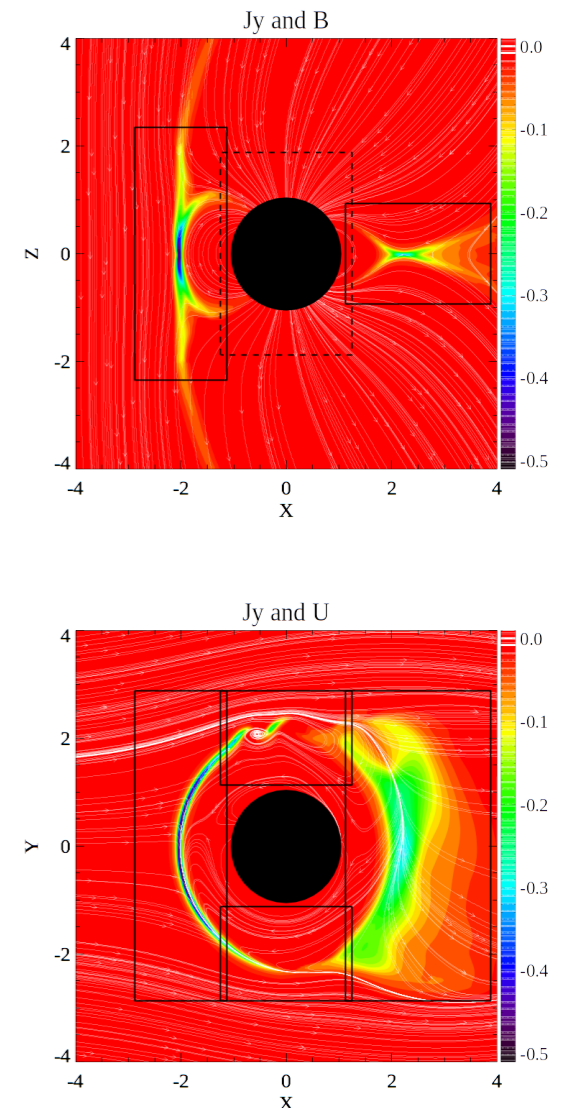


## Whistler Wave Test



Courtesy of L. Daldorff

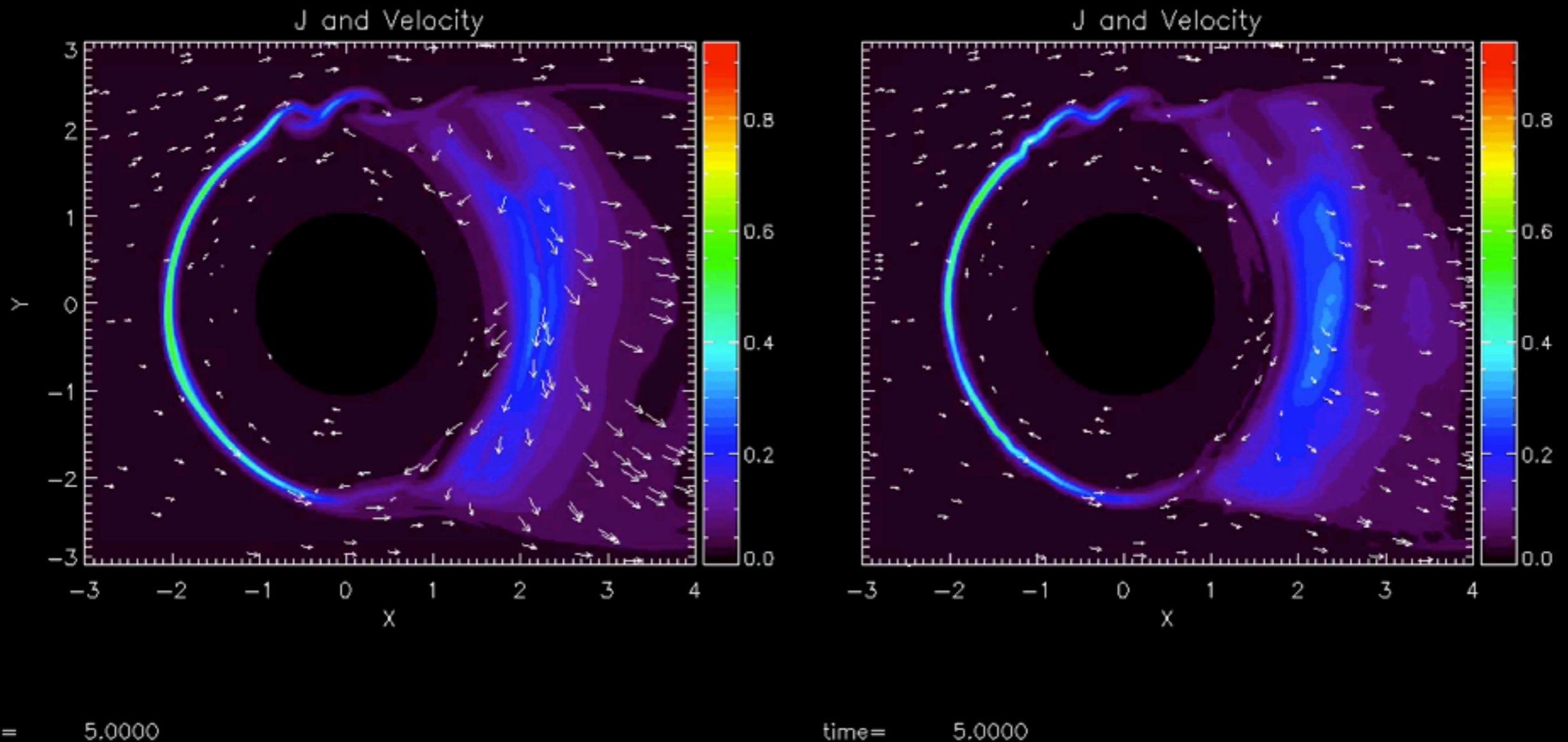
## Ganymede



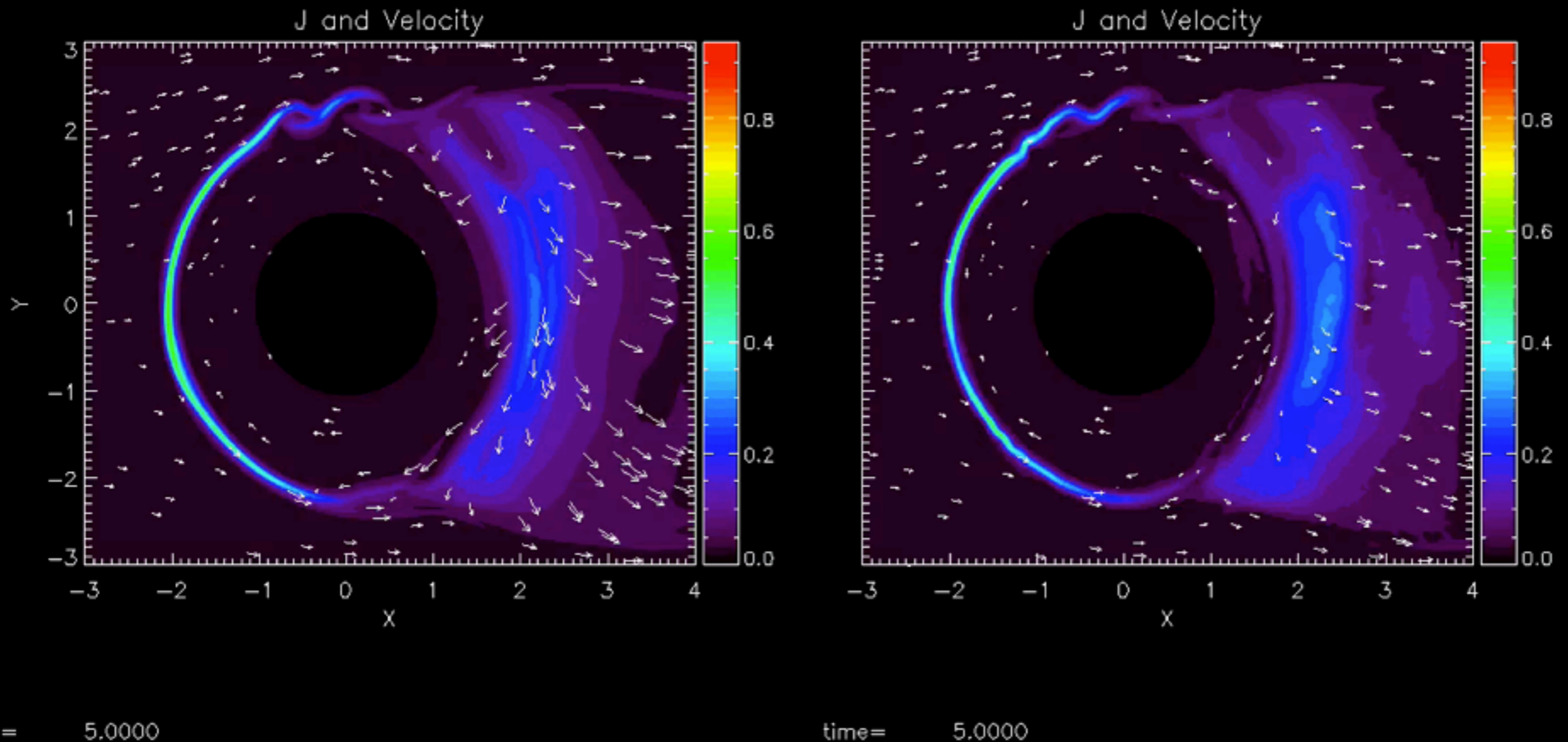
Courtesy of G. Toth

- 🌍 IPIC3D model is now embedded in BATSRUS (see *Daldorff et al., 2014*)
- 🌍 Numerical tests show the embedding behaves as expected.
- 🌍 Can use this to treat all the “interesting” regions of Ganymede and compare against the Hall solution.

# Comparing Hall MHD and EPIC-MHD

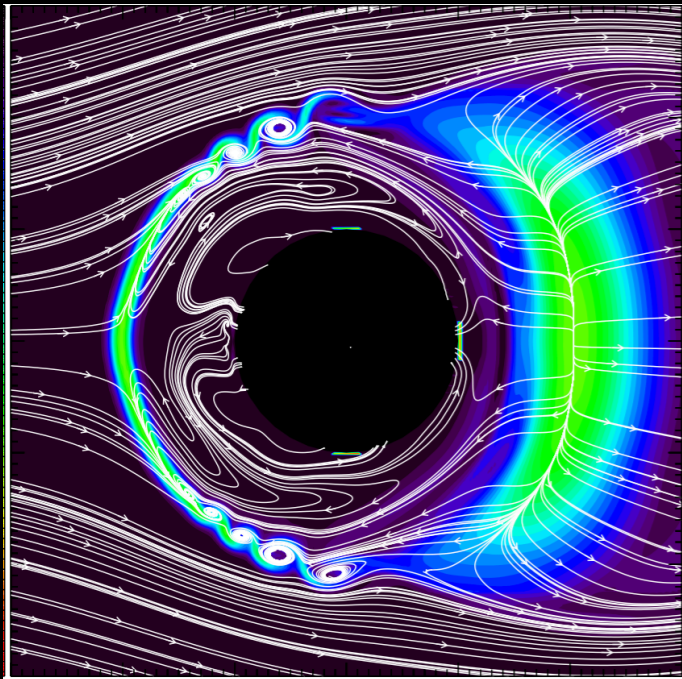


# Comparing Hall MHD and EPIC-MHD

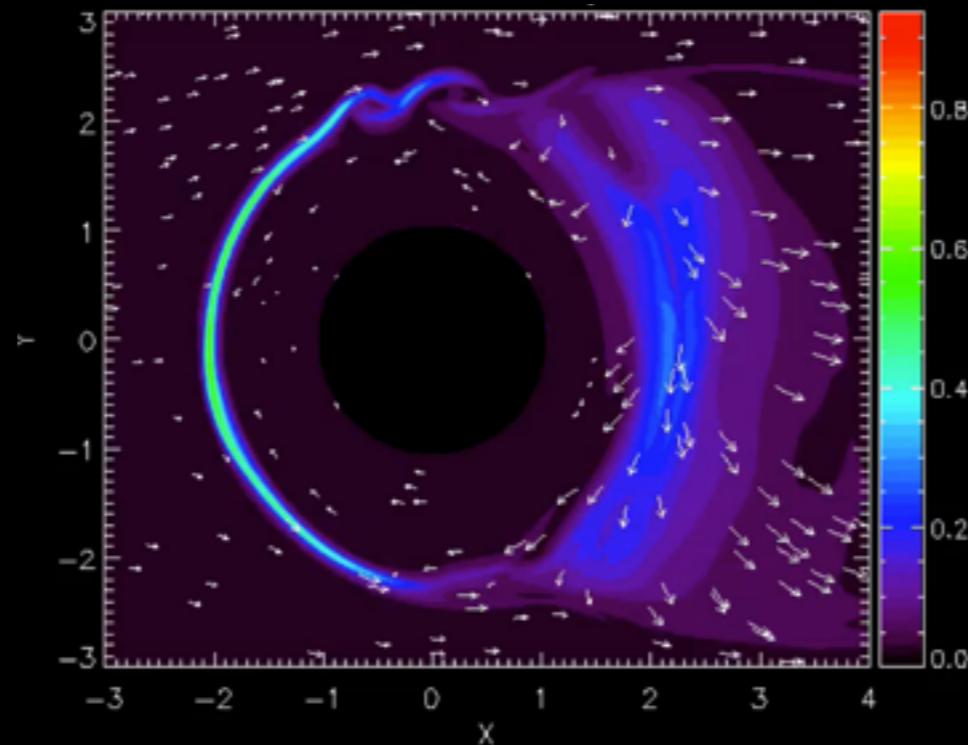


# An Analogy to the GEM Challenge

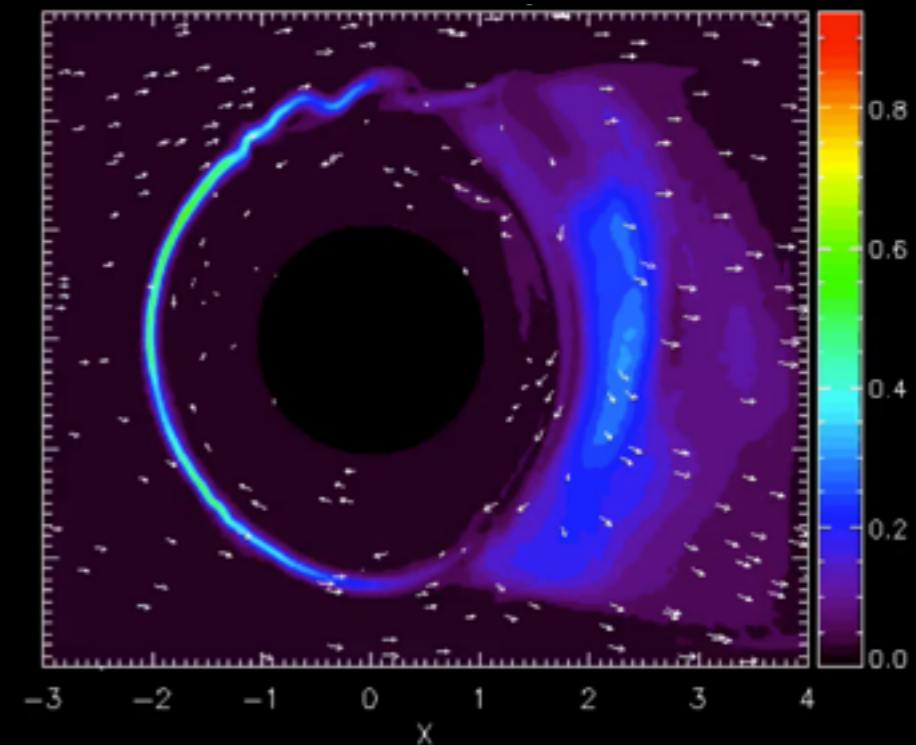
## Resistive MHD



## Hall MHD



## EPIC-MHD

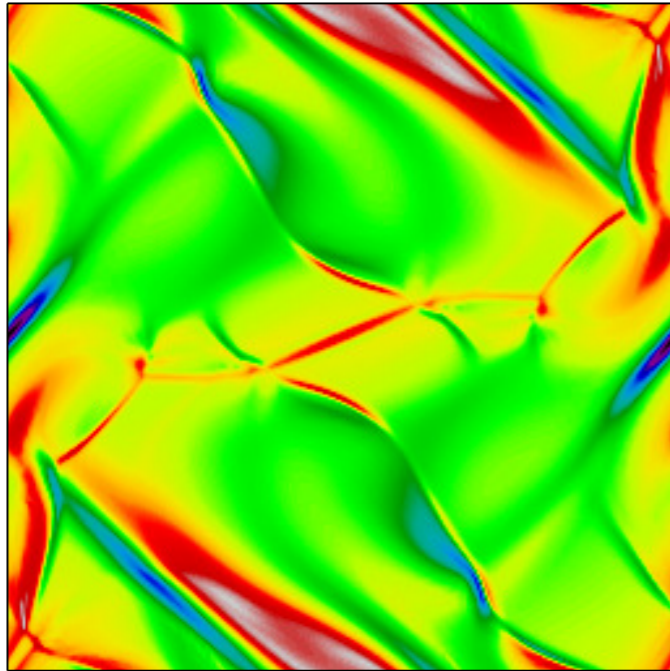


- In the GEM Reconnection Challenge many simulations were run with boundary conditions and initial conditions.
- All models with the Hall term gave fast reconnection.
- These results are like the GEM reconnection problem but with a real magnetosphere.
- Again, the Hall term seems to be the minimum extension of MHD that can capture the overall solution.

# Other Fluid Approaches to get Hall Physics

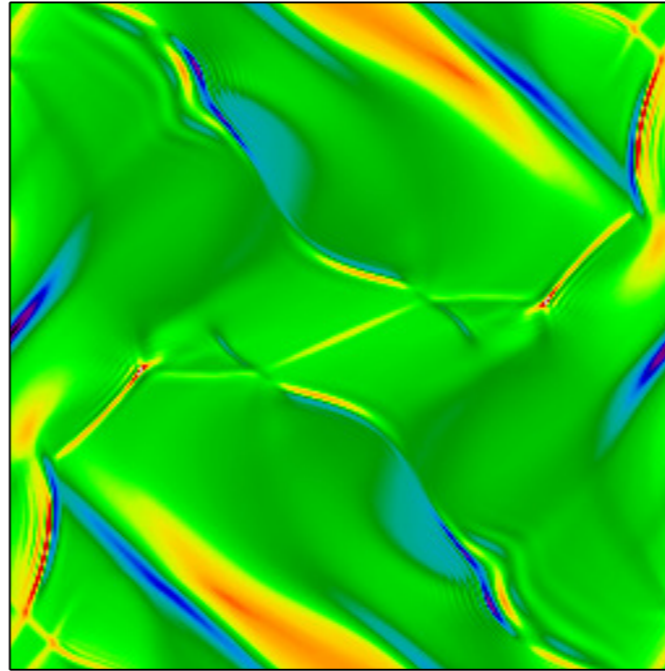
## Orszag-Tang Test

MHD:  $J_z$  at  $t=0.35$



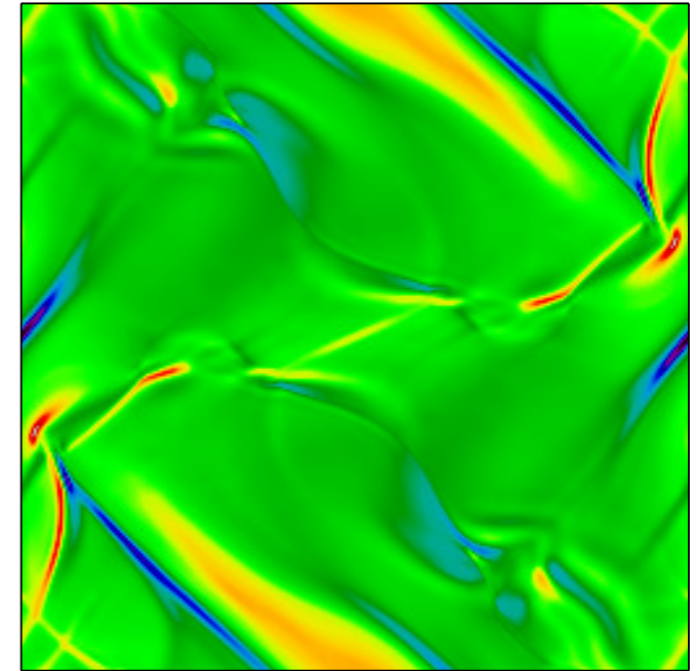
MHD

Hall MHD:  $J_z$  at  $t=0.34$



Hall-MHD

5-moment:  $J_z$  at  $t=0.34$



GKEYLL

*Courtesy of L. Wang*

- Solving a multifluid set of equations (ion and electron fluids) is an alternative way to the generalized ohm's law approach for including Hall physics.
- Orszag-Tang test shows similar results between Hall-MHD and multi fluid, but not MHD.
- The GKEYLL code from PPPL is currently being included into the OpenGGCM magnetosphere code.

# Conclusions

- 🌍 There is a very wide variety of modeling efforts on going in the community to capture the space environment system in all its complexity.
- 🌍 While there are some similarity of approaches, differences exist between the models shown here.
- 🌍 We have a long way to go to fully capture the multitude of scales and processes inherent in modeling the space environment system.

Thank You