

# Plasma Pressure Constraints on Magnetic Field Structure in the Substorm Growth Phase

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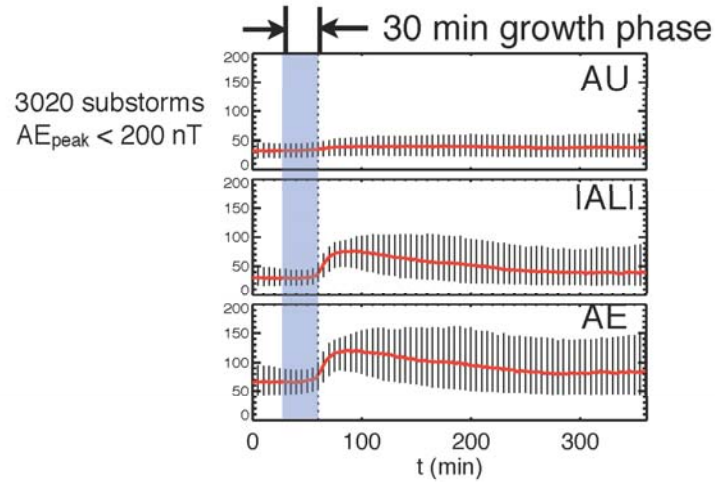
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# Motivation

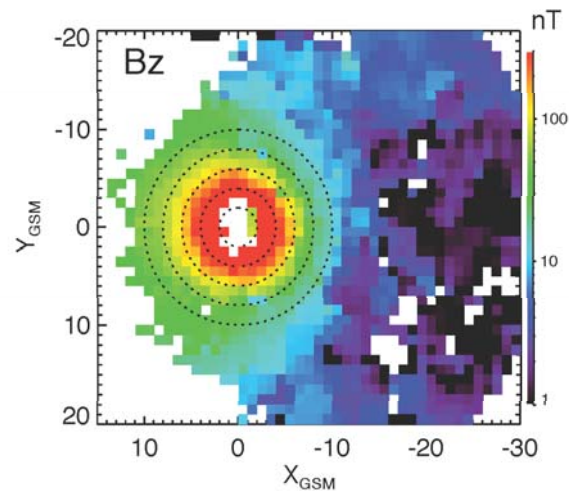
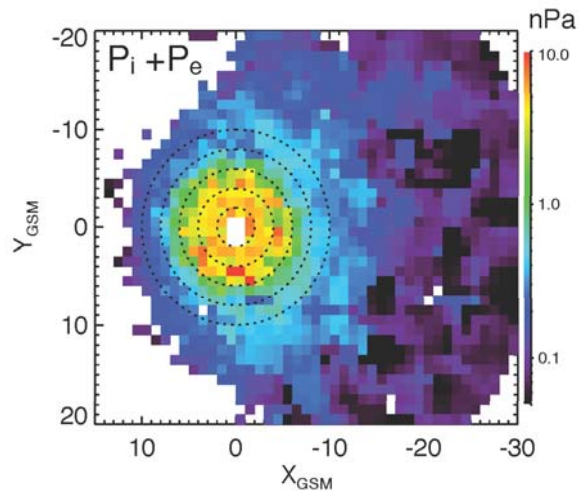
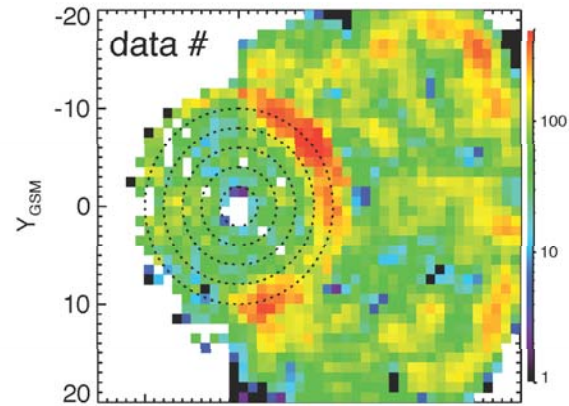
- I. Substorm growth phase
  - Gradual energy loading on **time scale  $\gg$  Alfvén time scale**
  - Configuration (magnetic field, electric current) not well described by existing models
- II. Large plasma beta (ratio of plasma pressure to magnetic pressure; values of 50 and higher [*Saito et al., GRL 2008*]) **plasma has strong influence on the field**
- III. Use growth phase observations to construct **empirical pressure model**
- IV. Use pressure model as **input to 3D force balanced magnetospheric model**

# THEMIS/Geotail Plasma Pressure

Substorms identified by Dr. Tung-Shin Hsu



Observations: THEMIS + Geotail  
(2007-2010) (1995-2005)



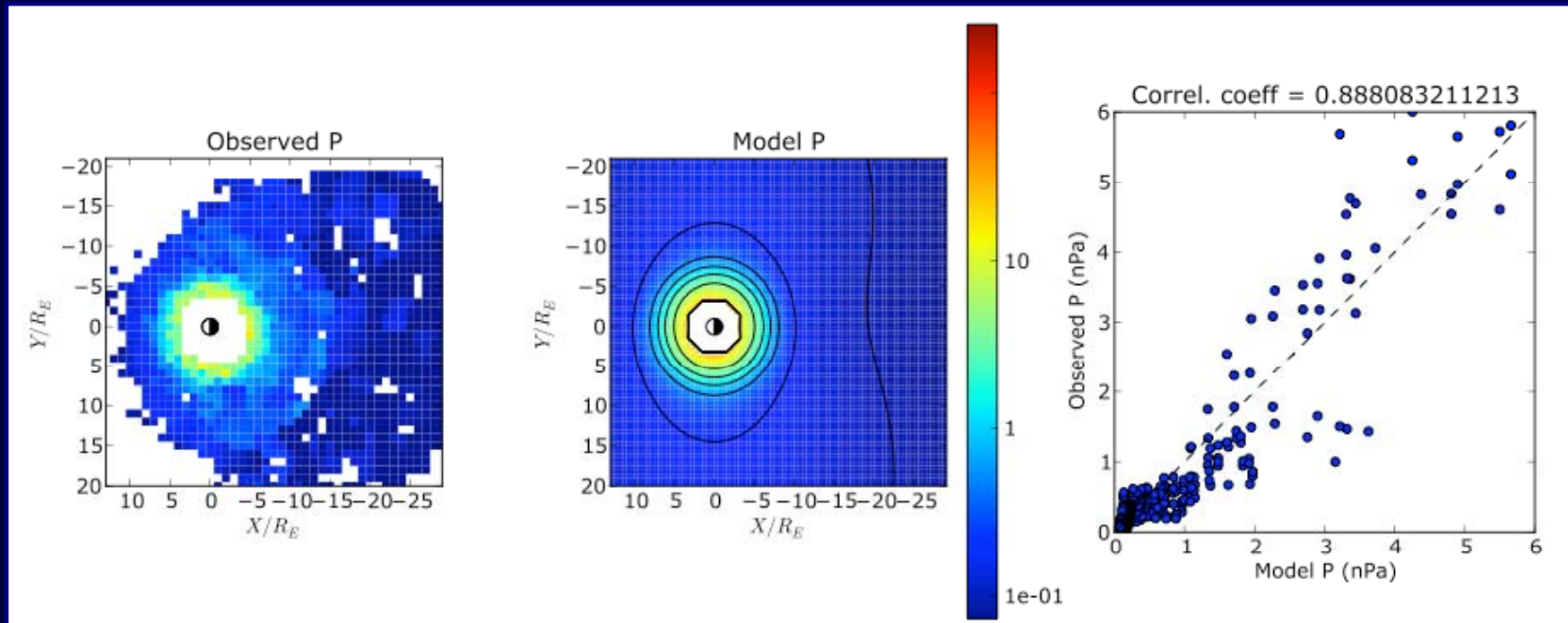
# Preliminary Results: Using THEMIS/Geotail Plasma Pressure

- Geotail + THEMIS growth phase data/binning by AE
- Smooth profile while capturing major features
- Nonlinear least square fit with constraints
  - $P > P_{\min}$
  - Bound constraints for coefficients a

$$P(R, \phi) = \exp(a_1 R) (a_2 + a_3 \sin \phi + a_4 \sin^2 \phi) + R^{b_1} (b_2 + b_3 \sin \phi + b_4 \sin^2 \phi)$$

- Global vs. Local Optimization; solution uniqueness
- Cf. *Tsyganenko and Mukai, [2003]*  
(no dawn/dusk asymmetry from Geotail data – LEP)

# THEMIS/Geotail P Fitting



- High correlation coefficient (cf. *Tsyganenko and Mukai, [2003]*)
- Dawn-dusk asymmetry in near-Earth region

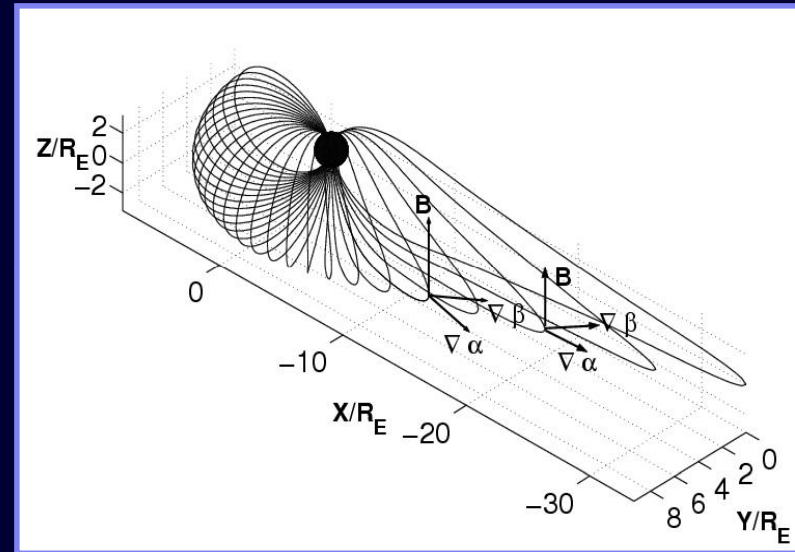
# 3D Equilibrium - Euler Potential Form

$$\mathbf{J} \times \mathbf{B} = \nabla P$$

- With isotropic pressure:  $P = P(\alpha, \beta)$
- De-composition along  $\mathbf{B} \times \nabla \alpha$  and  $\mathbf{B} \times \nabla \beta$

$$\mathbf{J} \cdot \nabla \alpha = \frac{1}{\mu_0} \nabla \cdot [(\nabla \alpha)^2 \nabla \beta - (\nabla \alpha \cdot \nabla \beta) \nabla \alpha] = -\frac{\partial P}{\partial \beta} \quad (1)$$

$$\mathbf{J} \cdot \nabla \beta = \frac{1}{\mu_0} \nabla \cdot [(\nabla \alpha \cdot \nabla \beta) \nabla \beta - (\nabla \beta)^2 \nabla \alpha] = \frac{\partial P}{\partial \alpha} \quad (2)$$



$$\mathbf{B} = \nabla \alpha \times \nabla \beta$$

- (1), (2) coupled Grad-Shafranov-like "quasi-2D" equations on const.  $\alpha$  and  $\beta$  surfaces; needed: pressure profile + magnetic boundary conditions
- Solution - in inverse form; magnetic field lines are explicit output (no need for integration etc.)

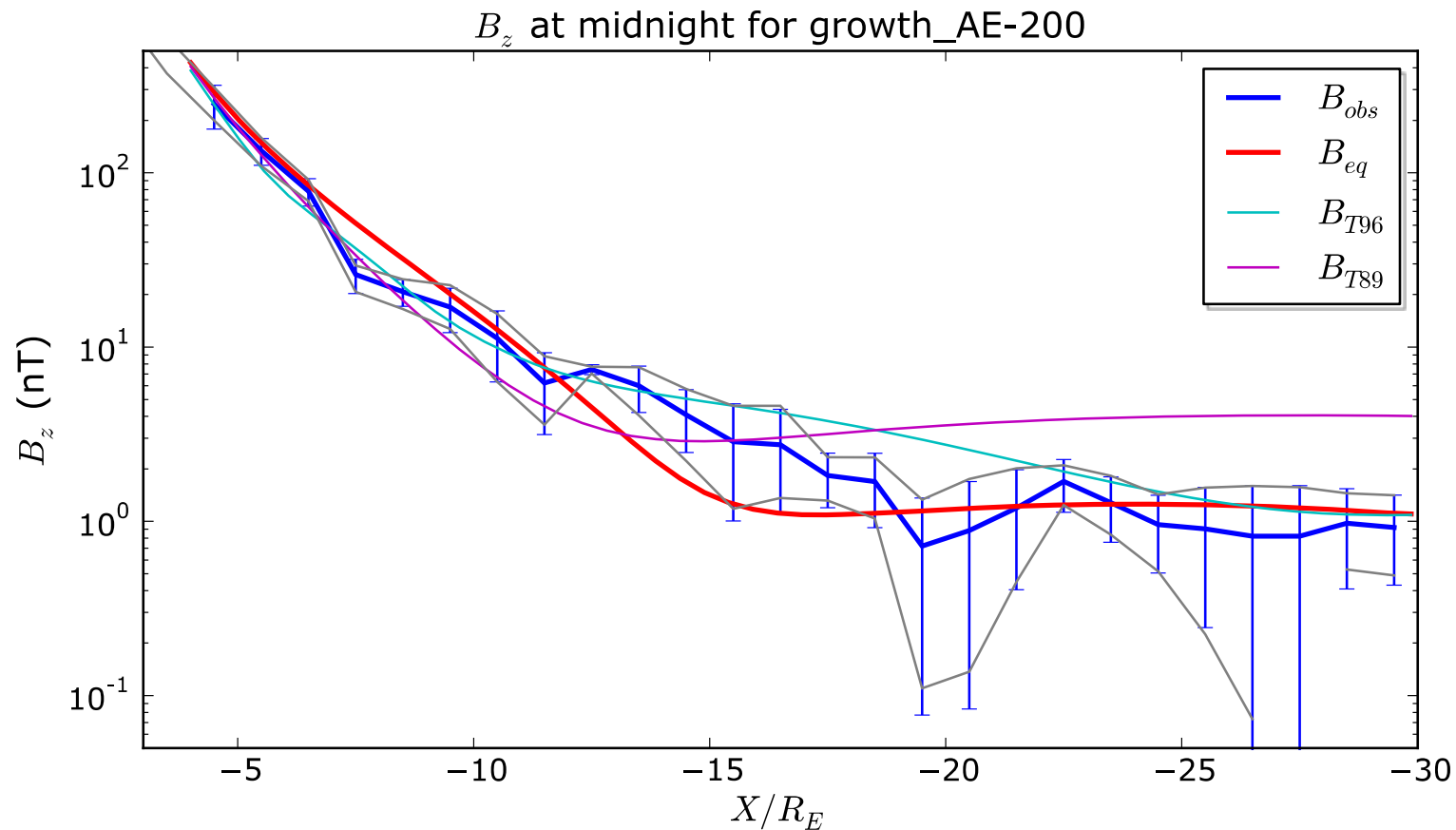
$$X(\alpha, \beta, \chi), Y(\alpha, \beta, \chi), Z(\alpha, \beta, \chi)$$

# Equatorial B-Field

Observed

Calculated

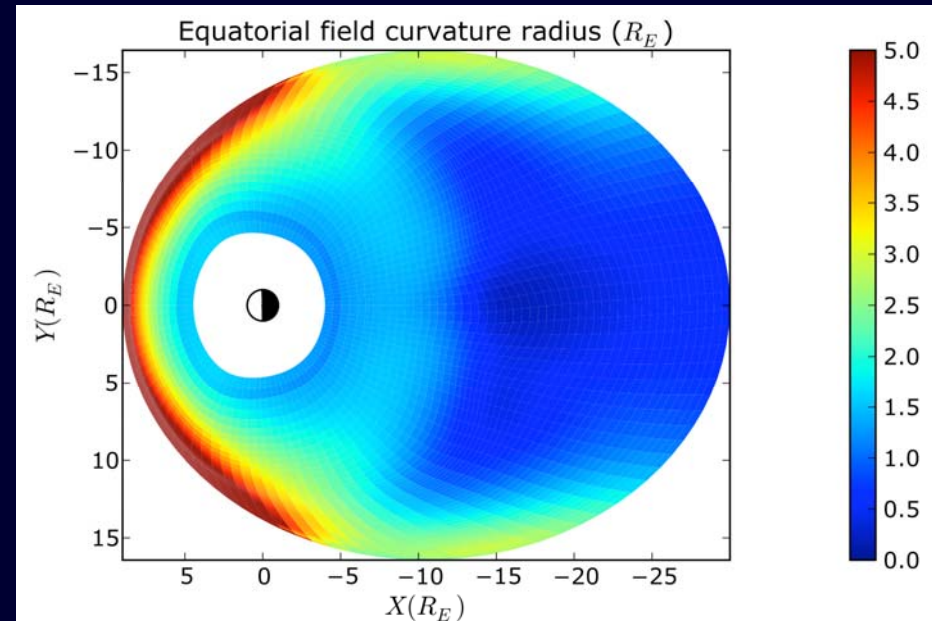
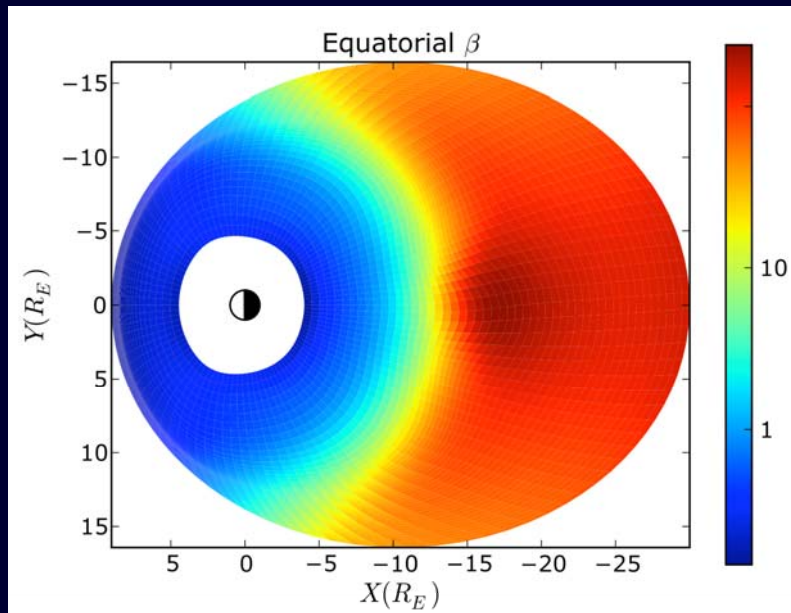
# B-Field on Midnight Meridian



- Observations not exactly at  $Z=0$ ; no realistic tilt in model
- T89, T96 fields too large at  $|X| > 15 R_E$  (not enough stretching)



# Plasma Beta and Field Curvature



$$\nabla \left( P + \frac{B^2}{2\mu_0} \right) = \frac{(\mathbf{B} \cdot \nabla) \mathbf{B}}{\mu_0} = \kappa B^2$$

$P$  = Plasma pressure

$B^2 / 2\mu_0$  = "Magnetic pressure"

$$\beta = 2\mu_0 P / B^2$$

$$R_c = \frac{1}{\kappa} \text{ Radius of curvature}$$

# Isotropy Boundary

Isotropy boundary – separating poleward region of energetic (> 30keV) particle isotropic precipitation from equatorward region of weak precipitation/loss-cone filling

Threshold condition  $R_c / \rho < 8$   
[Sergeev, 1993]

Remote sensing tool – proxy for field curvature

Future work: combine with low-altitude observations (DMSP, FAST)

